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Publication details, including instructions for authors and subscription information:
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To cite this article:
Lin William Cong, Xi Li, Ke Tang, Yang Yang (2023) Crypto Wash Trading. Management Science 69(11):6427-6454. https://doi.org/10.1287/mnsc.2021.02709

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MANAGEMENT SCIENCE
Vol. 69, No. 11, November 2023, pp. 6427–6454
ISSN 0025-1909 (print), ISSN 1526-5501 (online)

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# Crypto Wash Trading

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**Received:** August 19, 2021
**Revised:** October 8, 2022; April 13, 2023
**Accepted:** July 10, 2023
**Published Online in Articles in Advance:** September 19, 2023

**https://doi.org/10.1287/mnsc.2021.02709**

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**Abstract.** We present the first systematic approach to detect fake transactions on cryptocurrency exchanges by exploiting robust statistical and behavioral regularities associated with authentic trading. Our sample consists of 29 centralized exchanges, among which the regulated ones feature transaction patterns consistently observed in financial markets and nature. In contrast, unregulated exchanges display abnormal first significant digit distributions, size rounding, and transaction tail distributions, indicating widespread manipulation unlikely driven by a specific trading strategy or exchange heterogeneity. We then quantify the wash trading on each unregulated exchange, which averaged more than 70% of the reported volume. We further document how these fabricated volumes (trillions of dollars annually) improve exchange ranking, temporarily distort prices, and relate to exchange characteristics (e.g., age and user base), market conditions, and regulation. Overall, our study cautions against potential market manipulations on centralized crypto exchanges with concentrated power and limited disclosure requirements and highlights the importance of fintech regulation.

**History:** Accepted by David Simchi-Levi, Special Section of *Management Science*: Blockchains and Crypto Economics.

**Funding:** This research was partly funded by the Ewing Marion Kauffman Foundation [Grant G-201907-6995], the National Natural Science Foundation of China [Grants 72192802, 72192800, and 72192801], Ripple's University Blockchain Research Initiative (UBRI), and the FinTech at Cornell Initiative.

**Supplemental Material:** The online appendix and data are available at https://doi.org/10.1287/mnsc.2021.02709.

**Keywords:** Bitcoin • CeFi • cryptocurrency • forensic finance • fraud detection • regulation

## 1. Introduction

The combined market capitalization of all cryptocurrencies reached a peak of U.S. $3 trillion in late 2021 and, despite recent market crashes, still surpassed U.S. $1.2 trillion as of July 2023. The monthly crypto trading volume amounted to trillions of U.S. dollars (USD) in 2020, multiplying that of equity markets (Helms 2020). Both financial institutions and retail investors have had substantial exposure to the cryptocurrency industry (Bogart 2019, Fidelity 2019, Financial Conduct Authority 2019, Henry et al. 2019). Meanwhile, crypto exchanges, arguably the most profitable players in the ecosystem, remain mostly unregulated until recently. As of mid-2022, regulated exchanges (Coinbase, Bitstamp, Gemini, BitFlyer, itBit, etc.) only cover less than 3% of spot market transactions. In the process of vying for dominance in this lightly regulated market, crypto exchanges became increasingly vertically integrated in the absence of proper regulation and disclosure, resulting in incidents such as the FTX fraud (Q.ai 2022). Some exchanges also attempted to gain an advantage in unethical and legally questionable ways (Blockchain Transparency Institute 2019, Rodgers 2019, Vigna 2019). One such market manipulation is wash trading, whereby investors simultaneously sell and buy the same assets to create artificial transactions, distorting price and hurting investor confidence and participation as seen in other financial markets (Aggarwal and Wu 2006, Cumming et al. 2011, Imisiker and Tas 2018).

Against this backdrop, we provide to our knowledge the first systematic and rigorous study of misreporting and wash trading within this context. Our goal when we conducted the investigation in 2019 was to rigorously establish that wash trading is a widespread and systemic issue for the entire industry and to warn that centralized crypto exchanges can garner much market power and engage in harmful activities in the absence of regulatory scrutiny. Both issues have now occupied public attention given what has transpired in the crypto market over the past year. By inspecting the distribution of trade size, we document wash trading on most unregulated exchanges

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in late 2019, which, by our estimate, inflates reported transaction volume by more than 70% on average.[1] Furthermore, such misreporting and volume faking appear to improve the ranking and prominence of the exchanges; create short-term price dispersion across exchanges; occur more on newly established exchanges with smaller user bases; and have implications for long-term industrial organization, development, and regulations. In fact, our research contributes to the broad awareness of and actions for addressing the wash trading problem: regulators have increased scrutiny on wash trading, and several ranking websites, such as CoinMarketCap and CoinGecko, also changed their matrices from purely volume-based to more sophisticated ranking models, allowing filtering fake volumes using methodologies similar to or derived from ours.[2] The most recent Securities and Exchange Commission (SEC) allegation against Binance includes a wash trading accusation consistent with our findings.

Wash trading on centralized crypto exchanges warrants our attention for several reasons. First, crypto exchanges play an essential role in the industry (e.g., Amiram et al. 2021) by providing liquidity and facilitating price discovery just as in traditional exchanges. Many crypto exchanges have expanded into upstream (e.g., mining) and downstream (e.g., payment) sectors, consequently wielding significant influence as a complex of trading platforms, custodians, banks, and clearinghouses. Second, because liquidity begets liquidity, crypto exchanges have strong economic incentives to inflate trading volumes to increase brand awareness and ranks on third-party aggregator websites or media (e.g., CoinMarketCap, CoinGecko, Bitcointalk, and Reddit), which, in turn, increases the exchanges' profits from transaction fees.[3] Third, whereas wash trading is largely prohibited in most financial markets and developed economies (International Organization of Securities Commissions 2000), cryptocurrencies are particularly susceptible to wash trading under limited regulatory oversight. Online Appendix A contains more institutional details of crypto exchanges.

Whereas media and industry reports in 2018–2019 constitute whistleblowers, they were often imprecise and speculative (Fadilpasic 2019). Opinions on wash trading were divided, making practitioners and regulators unsure whether wash trading only concerned a few specific legal cases or was widespread.[4] We not only use rigorous statistical tools and intuitive behavioral benchmarks to demonstrate the existence of wash trading as an industry-wide phenomenon, but also provide suggestive evidence of the efficacy of regulation in this industry, which has implications for investor protection and financial stability, not to mention that the findings are also relevant for ongoing lawsuits and empirical research on cryptocurrencies, which frequently rely on transaction volumes. Finally, our research expands the applications of statistical and behavioral principles in forensic finance (Griffin and Kruger 2023) with regulatory implications for fintech and beyond.

Our first key finding is that wash trading is prevalent on unregulated exchanges but absent on regulated exchanges. To this end, we employ multiple methodologies that are successfully applied in natural and social science fields and are unlikely to be affected by specific trading strategies, exchange characteristics, or specificities of the asset class. We also advocate combining the various approaches for noise reduction and robust manipulation detection.

Specifically, we examine the distribution of the first significant digit for transactions on each exchange against Benford's law: a well-known statistical benchmark in natural and social sciences, widely used to detect fraud in fields such as macroeconomics, accounting, and engineering (e.g., Durtschi et al. 2004, Li et al. 2004). We next utilize a behavioral regularity in trading: clustering at transaction sizes at round numbers. Transactions cluster at round numbers, such as multiples of 10 in the decimal system, because they are cognitive reference points in decision making (Rosch 1975). Rounding is frequently observed in finance (Kandel et al. 2001, Kuo et al. 2015, Chen 2018), analysts' forecasts (Roger et al. 2018, Clarkson et al. 2020), currency trading (Osler and Savaser 2011), or London interbank offered rate submissions (Hernando-Veciana and Tröge 2020). Our third test explores whether the trade size distributions have fat tails characterized by power law as found in traditional financial markets and other economic settings (e.g., Gabaix et al. 2003a). We consistently find anomalous trading patterns on unregulated exchanges with higher ranked exchanges failing more than 20% of the tests and lower ranked exchanges failing more than 60%. Our findings remain robust in joint hypothesis tests.

We further quantify the fraction of fake volume by taking advantage of the rounding regularity. Illicit traders routinely employ program-generated fake orders with random order sizes to achieve scale without drawing attention (e.g., Vigna and Osipovich 2018, Rodgers 2019). Therefore, wash trades primarily generated by automated programs are likely to have low levels of roundness, that is, a larger effective number of decimals for trades. Authentic trades can be unrounded because of algorithmic trading or other transaction needs. We, thus, establish a benchmark ratio (based on calculations from the regulated exchanges) of unrounded trades to authentic trades with round sizes. We then consider any unrounded trades on unregulated exchanges beyond this ratio as wash trades.

We find that the volume of wash trading is, on average, as high as 77.5% of the total trading volume on unregulated exchanges with a median of 79.1%. In particular, wash trades on the 12 tier 2 exchanges are estimated to be more than 80% of the total trade volume, which is still

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more than 70% after accounting for observable exchange heterogeneity. These estimates, combined with the reported volume in Helms (2020), translate into wash trading of more than $4.5 trillion in spot markets and more than $1.5 trillion in derivatives markets in the first quarter of 2020 alone. To mitigate the influence of heterogeneity of traders and algorithmic trading strategies across various exchanges, we validate the roundness ratio estimation and conduct several robustness tests to allay selection concerns.

We next study exchange characteristics that correlate with wash trading and investigate the impact of wash trading on market outcomes, such as exchange ranking. Through proprietary data on historical rankings and trading volume information from CoinMarketCap, we discover that wash trading influences exchange ranking. Specifically, 70% of wash trading of total reported volume moves an exchange's rank up by 46 positions. An exchange's wash trading positively correlates with its cryptocurrency prices over the short term. Furthermore, exchanges with longer establishment histories and larger user bases wash trade less. Less prominent exchanges, in contrast, have short-term incentives for wash trading without drawing too much attention. Finally, wash trading is positively predicted by returns and negatively by price volatility.

Whereas current business incentives and ranking systems fuel the rampant wash trading on unregulated exchanges, regulated exchanges, which have committed considerable resources toward compliance and license acquisition and face severe punishments for market manipulation (Perez 2015), do little wash trading. We, thus, offer a concrete set of tools for regulation and third-party supervision in the crypto market for convincingly exposing wash trading and potentially combating non-compliant companies. The tests we introduce are not exhaustive, and wash traders may adjust their strategies in response to these tests. Nevertheless, our tools can still make transaction fabrications more difficult and regulation or litigation easier.

Our paper contributes to recent studies and regulatory debates on cryptocurrencies.[5] Amiram et al. (2021) is a closely related study that extends our framework to offer additional detection tools for wash trading, provides lower bounds using more recent data, and analyzes how competition interacts with exchange operations. Aloosh and Li (2023) is a complementary study that validates our detection methodology by showing individual traders clear their own orders using account-level data leaked from the now-closed Mt. Gox exchange. Victor and Weintraud (2021) find that wash trading worth 159 million U.S. dollars exists on decentralized exchanges such as EtherDelta and IDEX. Two other studies, Le Pennec et al. (2021) and Chen et al. (2022), follow our study to analyze crypto wash trading. The former introduces alternative detection tools, utilizing web traffic and wallet data, whereas the latter develops a matrix combining off-chain and on-chain data to examine five exchanges. Finally, Cong et al. (2023b) document crypto wash trading by individuals for tax-loss harvesting.

More broadly, our study belongs to the literature on manipulation and misreporting in finance.[6] Concerning cryptocurrency markets, Foley et al. (2019) study the illegal usage of cryptocurrencies; Gandal et al. (2018) and Griffin and Shams (2020) discuss manipulative behavior in Bitcoin (BTC) and Tether; Li et al. (2020), among others, document pump-and-dump patterns in various cryptocurrencies; and most recently, Choi and Jarrow (2020) discuss crypto bubbles caused by speculation or manipulation. These studies do not examine wash trading, which our unique and comprehensive data set enables us to do.

Our study is also among the first to discuss the effects of regulation on crypto exchanges, filling a void in the literature and offering new insights into cryptocurrency regulation. We further contribute to the debates on market concentration, collusion, and regulation in the blockchain industry (e.g., Cong and He 2019, Cong, He, and Li 2021, Roşu and Saleh 2021, Amiram et al. 2021, Capponi et al. 2023) by highlighting another detriment of vertical concentration of the operational scope of crypto exchanges. Relatedly, Irresberg et al. (2021) document that only a few blockchains dominate the public blockchain ecosystem. Without proper regulation and with vertical integration not seen in other markets, crypto exchanges may potentially engage in market manipulation or even outright fraud.

In terms of methodology, we enrich the use of and demonstrate the efficacy of statistical laws and behavioral principles for manipulation detection at scale in accounting and finance. Specifically, to our knowledge, we are the first to apply Benford's law, trade-size clustering, and power law in fintech and cryptocurrency studies. Our use of Pareto–Lévy distribution (instead of Zipf's law as seen in Mao et al. 2015, Prandl et al. 2017) for fraud detection is also novel in social sciences. Importantly, our findings imply that researchers using reported volumes by exchanges also need to heed the presence of wash trading and test the robustness of their conclusions.

The paper proceeds as follows. Section 2 describes our data and provides summary statistics. Section 3 presents the methodologies of wash trading detection and reports our empirical findings. Section 4 quantifies wash trading and details an array of tests to validate the methodology and demonstrate the robustness of the results. Section 5 relates wash trading to exchange characteristics, cryptocurrency returns, and exchange ranking before discussing its implications for regulation and industry practice. Section 6 concludes. The online appendices provide supplementary results and discussion, development and regulatory status of cryptocurrency exchanges, a theoretical model of wash trading, and further explanation of

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Benford's law as a forensic tool (available at https://ssrn.com/abstract=4529817).

## 2. Data and Summary Statistics

We collect cryptocurrency transaction information on 29 major centralized exchanges from the proprietary database maintained by TokenInsight (www.tokeninsight.com), a company specializing in consulting, rating, and research reports for cryptocurrency-related businesses. The selection of these exchanges was based on their publicity (rank on third-party websites), representativeness, and application programming interface compatibility, including well-known ones such as Binance, Coinbase, and Huobi as well as many obscure ones.[7] Our data cover the period from 00:00, July 9, 2019, to 23:59, November 3, 2019, and each transaction contains the exchange information, unique transaction ID, time stamp, price, amount of cryptocurrency traded, and trade pair symbol.[8] For each exchange, we focus on the four most widely recognized and heavily traded cryptocurrencies, BTC, Ethereum (ETH), Litecoin (LTC), and Ripple (XRP), which represent more than 60% of the volume and are available on almost all exchanges. The final sample contains 448,475,535 transactions. Other exchange-related variables, such as aggregated trading volume, reputation metrics, and exchange characteristics (e.g., exchange age, ranking, web traffic, etc.), are collected from official exchange websites and various data tracking and analysis platforms, including SimilarWeb, Alexa, and CoinMarketCap.

The New York State Department of Financial Services (NYSDFS), a regulatory entity in New York state, is one of the first agencies to establish regulation over cryptocurrencies and led the world in developing the regulatory framework for the cryptocurrency industry. Hence, we categorize the three exchanges (Bitstamp, Coinbase, and Gemini) with BitLicense issued and supervised by NYSDFS as regulated exchanges.[9] The other 26 noncompliant exchanges are classified as unregulated and divided into 10 tier 1 (including Binance) and 16 tier 2 exchanges based on their web traffic, which reflects an exchange's user base and reputation and plays essential roles in customer acquisition and competition. Specifically, tier 1 unregulated exchanges are the ones in the top 700 of the "SimilarWeb" website traffic ranking of the investment category during the sample period.[10] Our main findings are robust to using alternative regulatory frameworks around the world.[11]

Table 1 summarizes the characteristics of exchanges, including age, trading volume, and ranks from different metrics. The age for exchanges refers to the period from their establishment to July 2019. In Table 1, all the regulated exchanges have survived for at least five years. However, most unregulated tier 2 exchanges were launched in 2017 and 2018, whereas tier 1 exchanges are generally older.

In general, trade volume shows little correlation with our classification of exchanges: some unregulated exchanges have much larger trading volumes compared with regulated exchanges. For example, Coinbene, an unregulated tier 2 exchange, has a $50,944 million volume, whereas Coinbase's volume is only $15,212 million. The trading volume of different unregulated exchanges varies significantly. For instance, Exmo has only dozens of millions, whereas many unregulated exchanges exceed tens of billions.

Finally, we find regulated exchanges, especially Bitstamp and Gemini, rank behind many unregulated tier 1 exchanges based on web traffic. Coinbase has the highest trading volume among regulated exchanges and a better rank under both ranking algorithms. Regarding CoinMarketCap ranks based on trading volumes, seven unregulated tier 2 exchanges rank top 20 and outperform the majority of unregulated tier 1 and regulated exchanges. Although trading volume ranks cannot fully represent the quality and liquidity of exchanges, it is used by most ranking agencies. Thus, cryptocurrency investors are likely to choose an exchange according to these trading volume–based ranks. One anticipates that unregulated exchanges, especially those launched later, are motivated to engage in wash trading to achieve higher rankings and acquire more customers.

## 3. Empirical Evidence of Wash Trading

We present empirical evidence of crypto wash trading entailing four major trading pairs (BTC/USD, ETH/USD, LTC/USD, and XRP/USD).[12] Specifically, we examine the properties of trade sizes on each exchange and test them against three well-established statistical and behavioral benchmarks. The use of multiple tests at the exchange level demonstrates the presence of wash trading on unregulated exchanges robustly. As these tests are grounded in fundamental principles, they are least likely to be influenced by heterogeneous (yet authentic) trading specific to individual traders and exchanges. We further control this when quantifying the extent of wash trading in the subsequent section. It is important to note that each exchange may engage in wash trading using its unique approach (if it does so). Our implicit assumption is that large-scale wash trades during our sample period were not specifically designed to comply with all three or even some patterns. Because wash traders can learn from our work and adjust, we do not claim that these detection tools will remain effective indefinitely. However, without extensive coordination, it may be challenging for traders to fabricate transactions that pass all three tests simultaneously.

### 3.1. Distribution of First Significant Digits

Benford's law describes the distribution of the first significant digit in various naturally generated data sets, deriving from the intuition that many systems follow

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**Table 1.** Information on Crypto Exchanges

| Exchange code | Exchange age | Trade volume ($mil) | Ranking by web traffic: SimilarWeb Average rank in the investment section | Ranking by web traffic: SimilarWeb Average number of monthly visits (millions) | Ranking by web traffic: Alexa average Rank among all websites | Ranking by trade volume: CoinMarketCap |
|---|---|---|---|---|---|---|
| Panel A. Regulated exchanges | | | | | | |
| Bitstamp | A ≥ 5 | 1,466 | 473 | 1.872 | 14,297 | 63.7 |
| Coinbase | A ≥ 5 | 15,212 | 17 | 20.678 | 2,254 | 50.3 |
| Gemini | A ≥ 5 | 1,568 | 1,418.5 | 0.487 | 23,950 | 99.2 |
| Panel B. Unregulated tier 1 exchanges | | | | | | |
| Binance | 2 ≤ A< 5 | 41,936 | 21 | 18.770 | 1,630 | 10.5 |
| Bittrex | A ≥ 5 | 434 | 276 | 2.983 | 5,960 | 89.9 |
| Bitfinex | A ≥ 5 | 11,175 | 345 | 2.57 | 9,683 | 59.5 |
| HitBTC | A ≥ 5 | 34,157 | 498.5 | 1.363 | 9,815 | 27.9 |
| Huobi | A ≥ 5 | 38,789 | 285.5 | 1.673 | 8,379 | 22.7 |
| KuCoin | A < 2 | 4,005 | 255.5 | 1.879 | 8,663 | 55.2 |
| Liquid | A ≥ 5 | 545 | 699 | 0.394 | 13,357 | 53.3 |
| Okex | A ≥ 5 | 24,646 | 633 | 1.224 | 3,636 | 14.5 |
| Poloniex | A ≥ 5 | 975 | 38 | 2.146 | 768 | 95.6 |
| Zb | A ≥ 5 | 18,452 | 517.5 | 1.449 | 5,231 | 30.0 |
| Panel C. Unregulated tier 2 exchanges | | | | | | |
| Bgogo | A < 2 | 7,805 | 17,322 | 0.032 | 81,142 | 29.9 |
| Biki | A < 2 | 30,997 | N/A | 0.260 | 3,684 | 19.0 |
| BitZ | 2 ≤ A< 5 | 3,464 | 4,926.5 | 0.096 | 19,860 | 16.1 |
| Coinbene | A < 2 | 50,944 | 2,594 | 0.234 | 30,210 | 10.2 |
| DragonEX | A < 2 | 14,534 | 5,928.5 | 0.031 | 363,745 | 46.6 |
| Lbank | 2 ≤ A < 5 | 52,741 | 6,735 | 0.092 | 6,422 | 16.0 |
| Mxc | A < 2 | 34,624 | 2,770 | 0.265 | 6,306 | 11.9 |
| Fcoin | A < 2 | 21,848 | 1,818.5 | 0.092 | 100,223 | 15.0 |
| Exmo | 2 ≤ A < 5 | 52 | 961.5 | 0.919 | 37,634 | 90.0 |
| Coinmex | A < 2 | 2,756 | 11,567 | 0.007 | 1,684,659 | 6.6 |
| Bibox | A < 2 | 32,305 | 3,403.5 | 0.190 | 1,714 | 16.8 |
| Bitmart | A < 2 | 16,035 | 3,243 | 0.313 | 22,780 | 30.8 |
| Bitmax | A < 2 | 2,612 | 2,316.5 | 0.342 | 28,739 | 30.4 |
| Coinegg | 2 ≤ A < 5 | 16,668 | 10,350.5 | 0.032 | 53,000 | 21.3 |
| Digifinex | A < 2 | 23,525 | 3,061.5 | 0.188 | 1,858 | 16.0 |
| Gateio | A ≥ 5 | 2,013 | 1,096.5 | 1.065 | 2,808 | 73.7 |

*Notes.* This table demonstrates several characteristics of crypto exchanges in the data set. The exchange age is the duration from an exchange's establishment date to July 2019. Exchanges are categorized into three groups based on their length of survival: "more than five years," "between two and five years," and "less than two years." Trade volume is calculated as the sum of all transactions involving the four selected cryptocurrency pairs, that is, BTC, ETH, LTC, and XRP, all against U.S. dollars. SimilarWeb rankings are based on the SimilarWeb report over the period from August 2019 to October 2019, available at https://www.similarweb.com/. Alexa's ranking is accessed through https://www.alexa.com/siteinfo in November 2019. CoinMarketCap ranking is based on daily trade volume, calculated as daily average using proprietary data acquired from https://www.coinmarketcap.com during the sample period.

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multiplicative processes (e.g., Li et al. 2004). According to Benford (1938),

$$Prob(N \text{ is the first significant digit}) = \log_{10}(1 + N^{-1}),$$
$$N \in \{1, 2, 3, 4, 5, 6, 7, 8, 9\}. \quad (1)$$

The probability of one being the first significant digit is 30.10%. Digits two and three have probabilities of 17.60% and 12.50%, respectively. The probabilities of the rest (9.7%, 7.9%, 6.7%, 5.8%, 5.1%, and 4.6%, respectively) decrease as the digit increases. In Online Appendix B, we provide a theoretical derivation of the distribution of Benford's law and validate it for detecting wash trading through simulation.

In this section, we report whether the first significant digit distribution of transactions (denominated in the cryptocurrencies in question) conforms to the pattern implied by Benford's law (as shown in Equation (1)) on the 29 exchanges.[13] Inconsistency with Benford's law suggests potential data manipulations.

Figure 1 illustrates the first significant digit distributions for four cryptocurrencies with one regulated exchange and four unregulated exchanges. The five exchanges are the ones that fail the most tests in their categories and are consistently chosen throughout the paper for concise illustration. The distributions for the rest of the exchanges exhibit similar patterns and are shown in Online Appendix C. Bars show the fraction of transactions in which the trade size has integer $i$ as the first significant digit, and dots represent the frequency distribution implied by Benford's law.

For Coinbase, 32.75% of BTC trades and 32.73% of ETH trades have one as the leading digit, consistent with the benchmark frequency of 30.10% in Benford's law. Unregulated exchanges such as Fcoin and Exmo violate Benford's law with some first significant digits occupying a disproportionally large fraction, fitting our assumption of an incentivized wash trading campaign, which Fcoin and Exmo both offered in different formats.[14] Violations of another assumption, that is, exchange faking trade orders, can also be found in unregulated exchanges, such as Biki.

The first significant digit distributions of all regulated exchanges comply with Benford's law regardless of the type of cryptocurrency. Half of the unregulated exchanges, including tiers 1 and 2, exhibit apparent discrepancies with Benford's law in at least one type of cryptocurrency. Disconformity with Benford's law is observed on nine unregulated tier 2 exchanges, among which seven violate the law in at least two cryptocurrencies.

To quantitatively assess whether first significant digit distributions conform with Benford's law, we employ Pearson's chi-squared test. The value of the test statistic is calculated as

$$\chi^2 = \sum_{1}^{9} \frac{(O_i - E_i)^2}{E_i}, \quad (2)$$

in which $O_i$ is the observed distribution frequency and $E_i$ represents the value from Benford's law. In our study, trading data contains millions of observations in each trading pair of each exchange. The standard chi-square test will not work properly with a large sample size (Bergh 2015). We utilize the nominal value of distribution frequencies of the first significant digits to form a contestant approach through different subsamples. The null hypothesis is that the first significant digit distribution observed in an exchange's trading data are consistent with that of Benford's law.

As seen in Table 2, trades of regulated exchanges follow Benford's law, and so do those on most of the unregulated tier 1 exchanges. However, patterns for Bitfinex are inconsistent with Benford's law in BTC and XRP trades with a significance level of 1%. Moreover, five tier 2 exchanges (DragonEX, Mxc, Fcoin, Exmo, and Coinegg) significantly diverge from Benford's law in most cryptocurrencies. Other unregulated exchanges show sizable differences in several cryptocurrencies. For example, Liquid violates Benford's law in BTC at a 5% level; Biki and Coinmex fail in BTC and XRP at a 1% confidence level, respectively; Biki and BitZ fail at a 5% confidence level in ETH.

Overall, all regulated exchanges have transactions described by Benford's law. Meanwhile, 20% of unregulated tier 1 exchanges violate Benford's law in at least one cryptocurrency at a 5% significance level, and 50% of tier 2 exchanges fail to follow Benford's law in at least one cryptocurrency. The extent of violation observed here for a widely recognized forensic rule such as Benford's law may be surprising. However, there are a few reasons for this. First, unregulated exchanges might not consider the violation of Benford's law a serious issue in a largely unregulated industry. Faced with more pressing accusations, such as market manipulation and fraud, newly established small exchanges are unlikely to allocate resources to cover up wash trading traces. Some unregulated exchanges even publicly promote incentivized wash trading programs. Second, these exchanges may not be prepared for financial forensic tools as traditional institutions are. At the time we collected the data in 2019, Benford's law had not been extensively applied in the cryptocurrency industry. In the years since our initial draft, the situation has changed, and some exchanges might have incorporated Benford's law into their wash trading strategies.

### 3.2. Trade Size Clustering

We next examine the presence of clustering—traders' tendencies to use round trade sizes and round prices—within crypto exchanges. Clustering is a classic behavioral regularity frequently observed in financial markets. Grossman et al. (1997) propose a theory that the clustering in competitive markets with assets valued with great precision, such as the New York Stock Exchange, American

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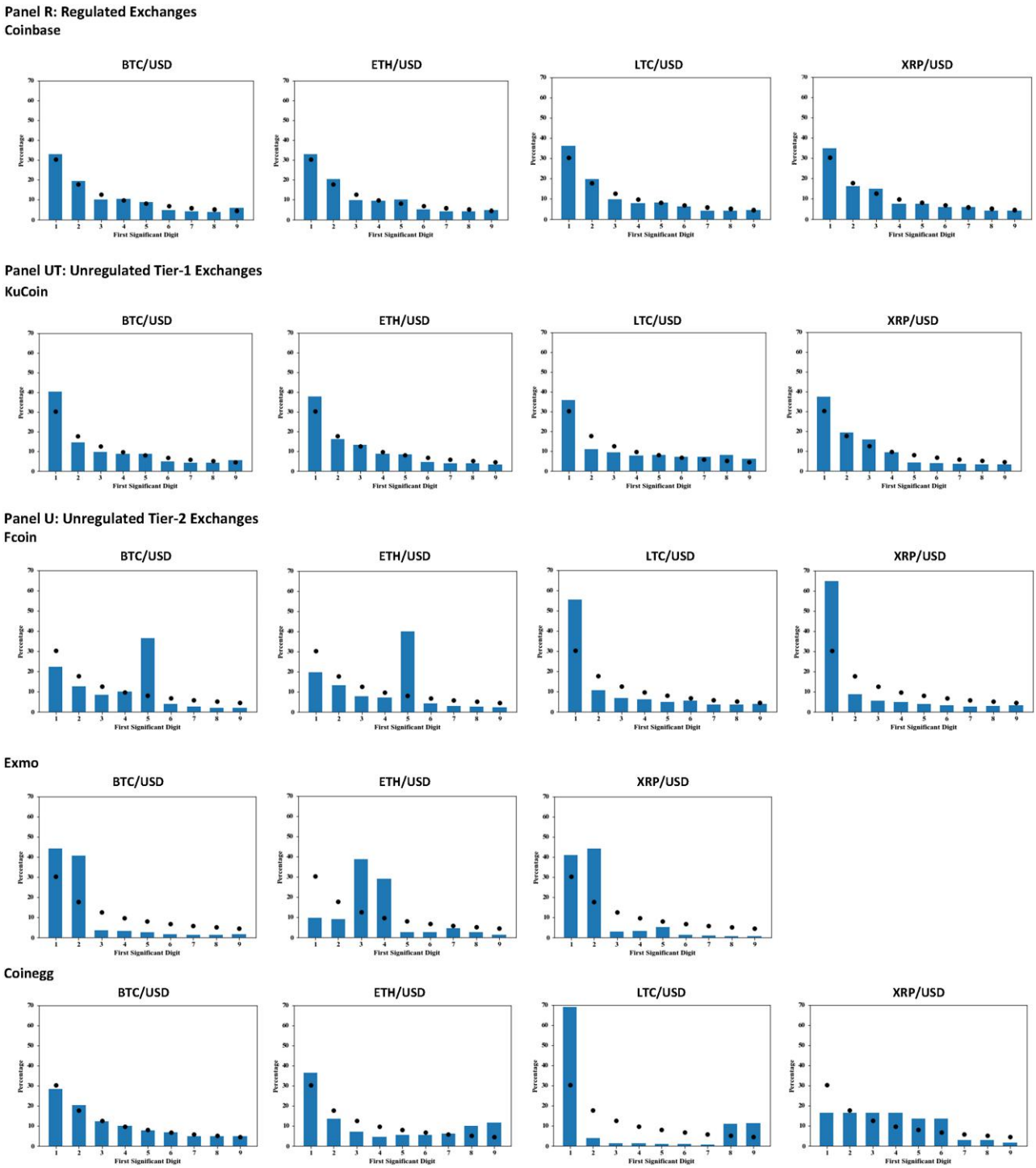
**Figure 1.** (Color online) First Significant Digit Distribution and Benford's Law




*Notes.* This figure displays the first significant digit distributions of trading data in bar charts. The dots represent distributions derived from Benford's law. Coinbase, KuCoin, Fcoin, Exmo, and Coinegg are five exchanges selected from regulated (panel R), tier 1 unregulated (panel UT), and tier 2 unregulated (panel U) exchanges, respectively.

Stock Exchange, and London Stock Exchange, is because of traders' attempts to minimize price negotiation and transaction costs. Clustering is also explained by psychology: authentic traders use round numbers as cognitive reference points (Rosch 1975) to simplify and save effort in decision making and evaluation (Ikenberry and Weston 2008, Lacetera et al. 2012, Kuo et al. 2015), distinguishing authentic trades from algorithmic trades (O'Hara et al. 2014, Mahmoodzadeh and Gençay 2017). Wash traders typically use automated trading programs,

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**Table 2.** Chi-Squared Test for Conformity with Benford's Law

| | BTC/USD | | ETH/USD | | LTC/USD | | XRP/USD | |
|---|---|---|---|---|---|---|---|---|
| Exchange | $\chi^2$ | $p$-value | $\chi^2$ | $p$-value | $\chi^2$ | $p$-value | $\chi^2$ | $p$-value |
| Panel A. Regulated exchanges | | | | | | | | |
| Bitstamp | 1.647 | 0.990 | 1.639 | 0.990 | 4.905 | 0.768 | 11.487 | 0.176 |
| Coinbase | 2.736 | 0.950 | 2.767 | 0.948 | 3.218 | 0.920 | 2.189 | 0.975 |
| Gemini | 3.304 | 0.914 | 0.698 | 1.000 | 1.969 | 0.982 | NA | NA |
| Panel B. Unregulated tier 1 exchanges | | | | | | | | |
| Binance | 2.495 | 0.962 | 4.113 | 0.847 | 4.645 | 0.795 | 7.205 | 0.515 |
| Bittrex | 1.464 | 0.993 | 2.620 | 0.956 | 6.117 | 0.634 | 0.748 | 0.999 |
| Bitfinex | 29.501*** | 0.000 | 5.349 | 0.720 | 7.157 | 0.520 | 47.121*** | 0.000 |
| HitBTC | 6.329 | 0.610 | 3.833 | 0.872 | 7.641 | 0.469 | 1.482 | 0.993 |
| Huobi | 6.832 | 0.555 | 3.104 | 0.928 | 1.094 | 0.998 | 0.468 | 1.000 |
| KuCoin | 5.969 | 0.651 | 4.100 | 0.848 | 7.386 | 0.496 | 7.790 | 0.454 |
| Liquid | 17.223** | 0.028 | 4.823 | 0.776 | NA | NA | 3.644 | 0.888 |
| Okex | 2.601 | 0.957 | 1.956 | 0.982 | 3.724 | 0.881 | 4.230 | 0.836 |
| Poloniex | 3.228 | 0.919 | 7.886 | 0.445 | 2.454 | 0.964 | 14.219* | 0.076 |
| Zb | 2.815 | 0.945 | 0.069 | 1.000 | 0.813 | 0.999 | 0.541 | 1.000 |
| Panel C. Unregulated tier 2 exchanges | | | | | | | | |
| Bgogo | 0.548 | 1.000 | 0.949 | 0.999 | NA | NA | NA | NA |
| Biki | 24.261*** | 0.002 | 16.677** | 0.034 | 6.505 | 0.591 | 4.371 | 0.822 |
| BitZ | 4.660 | 0.793 | 19.569** | 0.012 | 3.396 | 0.907 | 4.490 | 0.810 |
| Coinbene | 1.360 | 0.995 | 2.468 | 0.963 | 0.673 | 1.000 | 0.723 | 0.999 |
| DragonEX | 50.614*** | 0.000 | 8.254 | 0.409 | 124.881*** | 0.000 | 39.69*** | 0.000 |
| Lbank | 0.399 | 1.000 | 0.064 | 1.000 | NA | NA | NA | NA |
| Mxc | 5.088 | 0.748 | 23.086*** | 0.003 | 60.516*** | 0.000 | 15.300* | 0.054 |
| Fcoin | 114.788*** | 0.000 | 141.768*** | 0.000 | 31.068*** | 0.000 | 57.021*** | 0.000 |
| Exmo | 63.022*** | 0.000 | 122.298*** | 0.000 | NA | NA | 71.949*** | 0.000 |
| Coinmex | 10.771 | 0.215 | 4.662 | 0.793 | 12.325 | 0.137 | 26.135*** | 0.001 |
| Bibox | 2.430 | 0.965 | 7.140 | 0.522 | 4.115 | 0.847 | 7.602 | 0.473 |
| Bitmart | 0.544 | 1.000 | 0.122 | 1.000 | 1.042 | 0.998 | 14.676* | 0.066 |
| Bitmax | 1.157 | 0.997 | 2.583 | 0.958 | 11.614 | 0.169 | 4.815 | 0.777 |
| Coinegg | 0.678 | 1.000 | 23.351*** | 0.003 | 109.944*** | 0.000 | 26.835*** | 0.001 |
| Digifinex | 2.240 | 0.973 | 0.536 | 1.000 | 0.703 | 1.000 | 2.249 | 0.972 |
| Gateio | 1.695 | 0.989 | 0.924 | 0.999 | 1.317 | 0.995 | 0.577 | 1.000 |

*Notes.* The results in this table show whether trade size distributions of exchanges are consistent with the distribution of Benford's law. $\chi^2$ statistics and $p$-values are reported in the table.

***, **, and * denote the statistical significance levels at 1%, 5%, and 10%, respectively.

particularly when fake orders feature small transaction size yet substantial aggregate amounts (Vigna and Osipovich 2018, Rodgers 2019). As a result, wash trading inherently reduces the proportion of authentic volume and, thus, clustering.

As most cryptocurrencies can be traded in fractions and certain currencies possess larger unit values (particularly BTC), we establish, for the remainder of this paper, the smallest unit (base unit) as one unit in a specific decimal place value in proximity to one U.S. dollar. For instance, with the price of Bitcoin fluctuating between \$8,000 and \$10,000 in our sample period, most BTC/USD orders are below one BTC. In this context, round numbers in traditional financial markets such as 10, 100, or 10,000 are too substantial for individual traders. Considering the value of $10^{-4}$ BTC is within the order of magnitude of one U.S. dollar, it is deemed the base unit in this study. Similarly, the base units of other currencies are 0.001 ETH, 0.01 LTC, and 1 XRP, respectively.

We now examine whether trade-size clustering appears at multiples of 100 base units for each cryptocurrency.[15]

Figure 2 depicts trade size distributions of representative exchanges in two observation ranges for BTC, ETH, LTC, and XRP, highlighting the clustering effect at round sizes. Online Appendix D presents the histograms of the remaining exchanges.

Trade data from regulated exchanges display a downward-sloping curve with prominent peaks at multiples of 5,000 base units in the range of 0–10 BTC (e.g., 0.5 BTC, 1 BTC, 1.5 BTC, 2 BTC, etc.). Similar patterns also appear in distributions of ETH, LTC, and XRP. These findings suggest the presence of trade size clustering on regulated crypto exchanges, consistent with the trade patterns in regulated financial markets, which display a downward trend because large orders are less frequently placed and executed, as well as a trade size clustering effect (e.g., Moulton 2005, Alexander and Peterson 2007, ap Gwilym and Meng 2010,

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**Figure 2.** Trade-Size Clustering

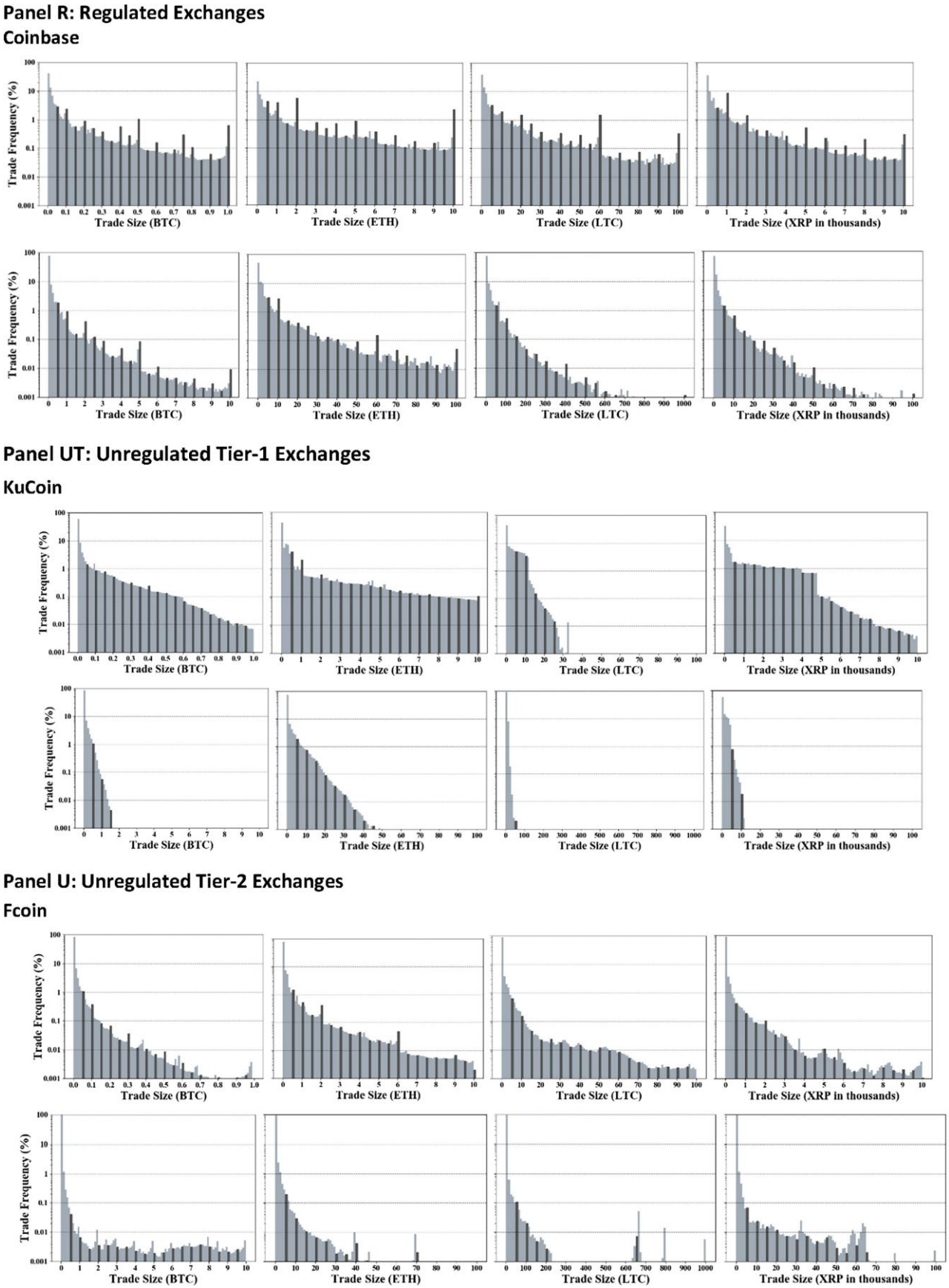

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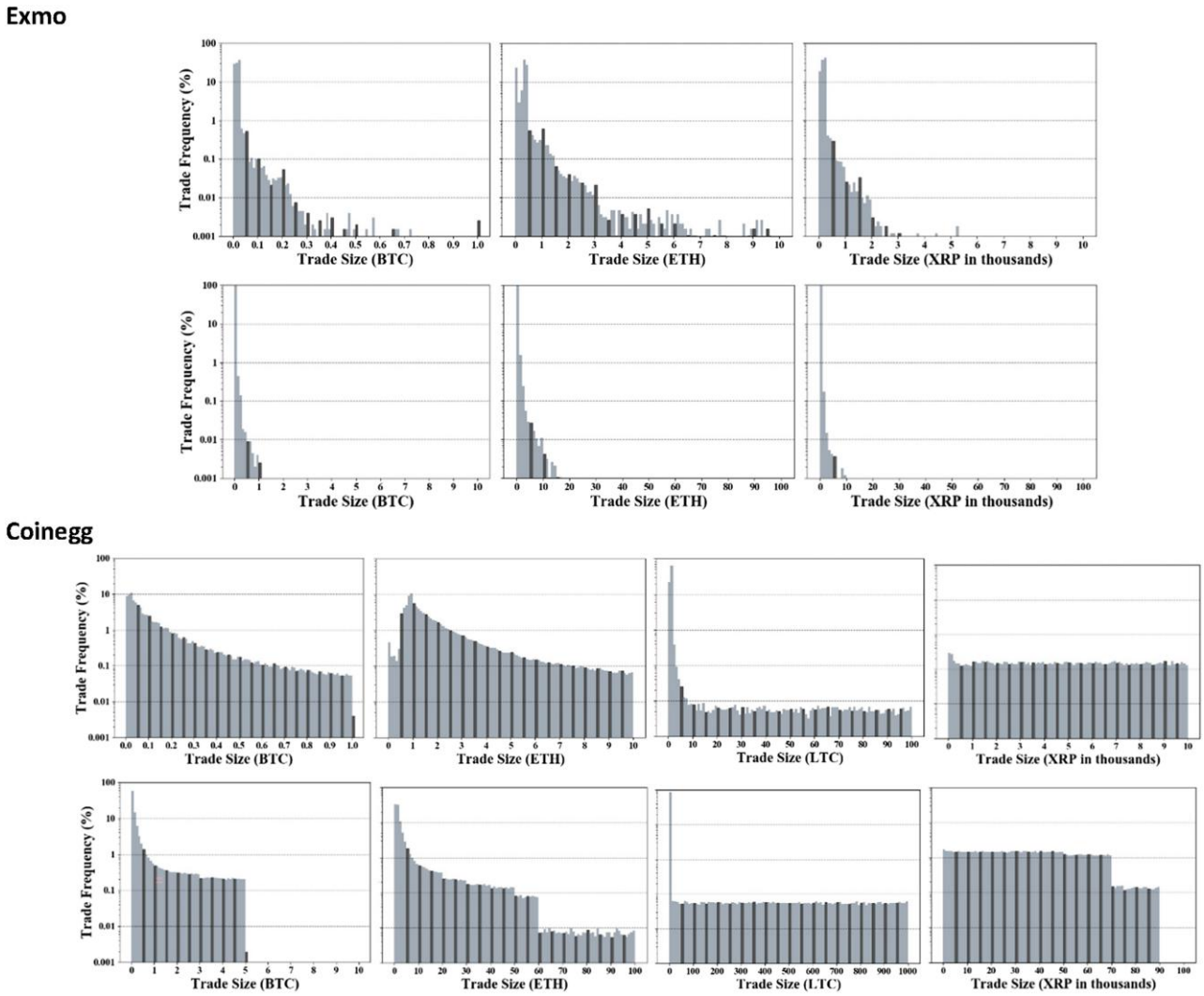
**Figure 2.** (Continued)




*Notes.* The clustering effect in trade-size distribution histograms on sample exchanges. Two sets of observation ranges are applied for each trading pair: 0–1 BTC, 0–10 BTC, 0–10 ETH, 0–100 ETH, 0–100 LTC, 0–1,000 LTC, 0–10,000 XRP, and 0–100,000 XPR. In each histogram, we highlight every 5th and 10th bin to illustrate the clustering effect.

Verousis and ap Gwilym 2013, Mahmoodzadeh and Gençay 2017).

On the other hand, trade size distributions of unregulated exchanges demonstrate some abnormal patterns. Taking KuCoin in Figure 2 as an example, it does not show a clear clustering pattern in round number trades. Besides, most trades of KuCoin are concentrated at small sizes and display an anomalous drop in frequency, especially in LTC and XRP trades. Moreover, clustering patterns for different assets vary across crypto exchanges and show no overall pattern. On unregulated tier 2 exchanges, we observe less apparent clustering at round sizes, and trade patterns vary dramatically, deviating from the typical downward distribution. For instance, when examining larger ranges, trade frequency on Fcoin does not monotonically change with the increase in trade size for all cryptocurrency trades. Similar issues are observed on other exchanges (refer to Online Appendix D; e.g., DragonEX, Mxc, and Digifinex in BTC trades; BitZ, Mxc, Bibox, and Digifinex in ETH trades). Additionally, abnormal patterns, such as gaps, cliffs, scarce peaks, and uniform distributions, can be observed in unregulated exchanges, which are contrary to the behavioral regularity in financial markets.

To quantify the effect of trade-size clustering, we conduct Student's $t$-test for each crypto exchange by comparing trade frequencies at round trade sizes with the highest frequency of nearby unrounded trades. The value of the test statistic is calculated as

$$t = \frac{\overline{x} - \mu_0}{s/\sqrt{n}}, \tag{3}$$

where $\overline{x}$ is the average of rounded trade frequencies minus unrounded trade frequencies, $s$ is the sample

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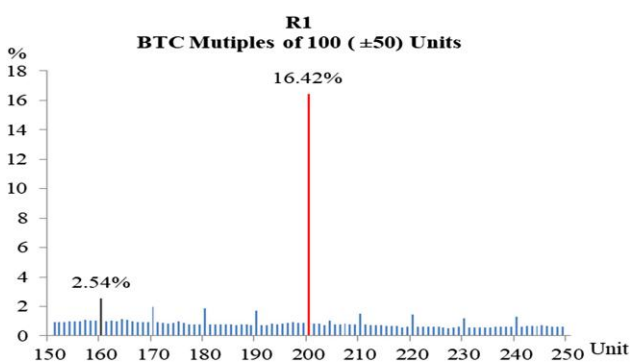
standard deviation, and $n$ is the sample size. The null hypothesis of the test is that the difference between frequencies at rounded numbers and nearby unrounded trades is zero.

For each trading pair, we set up two sets of observation windows: windows centered on multiples of 100 units (100X) with a radius of 50 units (100X − 50, 100X + 50) and windows centered on multiples of 500 units (500Y) with a radius of 100 units (500Y − 100, 500Y + 100). Trade frequency is calculated as the number of transactions with size $i$ over total transaction numbers in the observation window. For example, Figure 3 illustrates that, in BTC transactions on Bitstamp, the observation window of around 200 units (0.02 BTC) ranges from 150 units to 250 units (0.015–0.025 BTC). Orders at 0.02 BTC constitute 16.42% of the total within the entire observation window, whereas the highest trade frequency of unrounded orders is only 2.54%. The apparent difference indicates that orders within the 0.015–0.025 BTC window cluster at 0.02 BTC.

Table 3 presents the results of $t$-tests for size clustering on regulated exchanges (panel A) and unregulated tier 1 (panel B) and tier 2 exchanges (panel C). As anticipated, trade frequency at round sizes is significantly higher than at unrounded sizes across all three regulated exchanges regardless of the cryptocurrencies and observation ranges examined. This finding aligns with the observations in Figure 2. Additionally, in terms of difference and $t$-statistics, size clustering is more evident at multiples of 500 units. For example, when looking at BTC trades on Bitstamp, the difference in frequency is 9.1% in trade size of multiples of 100 units (e.g., 0.01 BTC, 0.02 BTC, and 0.03 BTC), whereas the difference is 20.3% at sizes that are the common multiples of 500 units (e.g., 0.05 BTC, 0.10 BTC, 0.15 BTC).

**Figure 3.** (Color online) Illustration of the $t$-Test for Clusters




*Notes.* Trade frequencies at round trade sizes are tested against unrounded trade sizes nearby. Frequency for trade size $i$ is calculated as the number of trades with size $i$ over the total number of trades in an observation window (e.g., $i - 50$ to $i + 50$). Frequencies at round trade sizes (e.g., the 200th unit) and the highest frequencies of nearby unrounded trades (e.g., the 160th unit) are recorded as a pair. The $t$-test on the difference between round and unrounded frequencies in a pair is then carried out over a sample of all pairs.

As with regulated exchanges, three unregulated tier 1 exchanges (Bitfinex, Liquid, and Poloniex) show positive and significant differences at a 1% level in trades of all available cryptocurrencies (except for XRP on Poloniex, which is significant at 5%). Trade clustering also appears more frequently at multiples of 500 units. For example, six tier 1 exchanges (Binance, Bitfinex, Huobi, Liquid, Okex, and Poloniex) display noticeable clustering effects at multiples of 500 units for all four cryptocurrencies. However, KuCoin and Zb show insignificant differences in frequencies between round and unrounded trades.

In contrast, clustering at round sizes is largely absent on unregulated tier 2 exchanges. Half exchanges exhibit no sign of clustering for all cryptocurrencies in both observation windows. Except for Bitmax, all tier 2 exchanges have no clustering in at least one cryptocurrency. Besides, on some exchanges, trade clustering becomes less evident at a higher level of roundness (multiples of 500 units). For example, on BitZ and DragonEX, frequencies at multiples of 100 units are higher (significantly at a 1% level), but clusters at multiples of 500 units are insignificant.

We also regress the (logit) percentage of trades at certain sizes on various dummy variables, which are set to one at round sizes. Online Appendix E reports the consistent findings.

In summary, we observe that regulated exchanges display an evident clustering effect in transaction size, whereas unregulated tier 1 and 2 exchanges exhibit little clustering with 30% and 50% of exchanges showing no trade size clustering in all cryptocurrencies, respectively. It is important to note that clustering involves rounding off the last nontrivial digits and affects little the distribution of the first significant digit. As we are only applying the plain vanilla Benford's law concerning the distribution of the first significant digits (not the first two or three significant digits), there is no interference with the clustering tests.[16]

### 3.3. Tail Distribution

We next examine the tails of trade-size distributions on each crypto exchange. In economics and finance, power law is found to capture the "fat tails" of many distributions.[17] Mathematically, power-law distribution has a cumulative density function

$$P(X > x) \sim x^{-\alpha}, \tag{4}$$

where $\alpha$ is known as the power law exponent or the tail exponent. When using the probability density function, the relevant parameter is $\alpha_{pdf} = \alpha + 1$.

One explanation for the power law tails in financial data are the trading behavior of large investors who try to avoid large price impacts in the markets (Gabaix et al. 2003a). Other studies attribute them to the investors' limited information on the value of assets (Kostanjčar and Jeren 2013, Nirei et al. 2020) and herding (Nirei et al. 2020). Specifically, for trade volume, several previous

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**Table 3.** Student's *t*-Tests for Trade Size Clustering

Observation range: Multiples of 100 units (100× − 50, 100× + 50)

| | BTC/USD | | ETH/USD | | LTC/USD | | XRP/USD | |
|---|---|---|---|---|---|---|---|---|
| Exchange | Difference | *t* statistics | Difference | *t* statistics | Difference | *t* statistics | Difference | *t* statistics |
| Panel A. Regulated exchanges | | | | | | | | |
| Bitstamp | 0.091*** | 14.490 | 0.112*** | 12.280 | 0.160*** | 10.767 | 0.063*** | 6.726 |
| Coinbase | 0.089*** | 14.875 | 0.135*** | 15.647 | 0.109*** | 8.945 | 0.032*** | 2.955 |
| Gemini | 0.125*** | 13.655 | 0.119 | 9.713 | 0.203*** | 8.284 | NA | NA |
| Panel B. Unregulated tier 1 exchanges | | | | | | | | |
| Binance | 0.188*** | 16.993 | 0.226*** | 20.740 | 0.179*** | 9.310 | 0.005 | 0.540 |
| Bittrex | 0.026* | 1.926 | 0.039** | 2.327 | 0.065*** | 2.943 | 0.076*** | 3.952 |
| Bitfinex | 0.100*** | 12.654 | 0.078*** | 8.655 | 0.110*** | 6.696 | 0.076*** | 5.681 |
| HitBTC | 0.005 | 1.073 | −0.002 | −0.568 | 0.004 | 0.644 | −0.005 | −0.556 |
| Huobi | 0.128*** | 16.895 | 0.083*** | 14.442 | 0.104*** | 8.003 | 0.010 | 1.116 |
| KuCoin | −0.015 | −2.668 | −0.001 | −0.081 | −0.003 | −0.089 | −0.014 | −1.379 |
| Liquid | 0.088*** | 6.854 | 0.057*** | 3.685 | NA | NA | 0.132*** | 6.498 |
| Okex | 0.082*** | 12.620 | 0.067*** | 10.614 | 0.047*** | 5.289 | 0.009 | 0.903 |
| Poloniex | 0.084*** | 10.192 | 0.060*** | 5.782 | 0.101*** | 4.018 | 0.054** | 2.570 |
| Zb | −0.013 | −4.119 | −0.016 | −18.635 | −0.030 | −9.173 | −0.020 | −16.206 |
| Panel C. Unregulated tier 2 exchanges | | | | | | | | |
| Bgogo | −0.016 | −86.208 | −0.022 | −7.374 | NA | NA | NA | NA |
| Biki | −0.015 | −24.733 | −0.014 | −12.297 | −0.017 | −27.701 | −0.017 | −34.675 |
| BitZ | 0.030*** | 7.110 | 0.029*** | 3.687 | −0.002 | −0.131 | −0.083 | −2.264 |
| Coinbene | −0.008 | −5.629 | −0.015 | −5.415 | −0.012 | −2.601 | −0.008 | −1.019 |
| DragonEX | 0.073*** | 6.573 | −0.027 | −7.279 | −0.015 | −13.844 | −0.014 | −11.199 |
| Lbank | −0.020 | −33.174 | −0.022 | −52.875 | NA | NA | NA | NA |
| Mxc | 0.019* | 1.952 | 0.096*** | 9.019 | 0.058*** | 9.982 | −0.017 | −15.221 |
| Fcoin | −0.001 | −0.341 | 0.035*** | 6.552 | −0.005 | −0.804 | −0.008 | −1.207 |
| Exmo | 0.106** | 2.313 | 0.032 | 1.038 | NA | NA | −0.022 | −0.450 |
| Coinmex | −0.004 | −5.622 | −0.015 | −11.549 | −0.016 | −12.730 | −0.015 | −22.775 |
| Bibox | 0.259*** | 20.279 | 0.123*** | 31.466 | 0.111*** | 15.258 | −0.017 | −16.156 |
| Bitmart | −0.015 | −13.164 | −0.014 | −15.846 | −0.021 | −15.304 | −0.035 | −3.158 |
| Bitmax | 0.034*** | 3.411 | 0.061*** | 8.316 | 0.094*** | 5.662 | 0.083*** | 6.503 |
| Coinegg | −0.032 | −22.436 | −0.021 | −33.123 | −0.036 | −16.175 | −0.033 | −2.149 |
| Digifinex | −0.015 | −8.266 | −0.015 | −8.765 | −0.018 | −35.684 | −0.017 | −30.582 |
| Gateio | 0.243*** | 20.575 | 0.019** | 2.354 | 0.018* | 1.753 | 0.004 | 0.333 |

Observation range: Multiples of 500 units (500× − 100, 500× + 100)

| | BTC/USD | | ETH/USD | | LTC/USD | | XRP/USD | |
|---|---|---|---|---|---|---|---|---|
| Exchange | Difference | *t* statistics | Difference | *t* statistics | Difference | *t* statistics | Difference | *t* statistics |
| Panel A. Regulated exchanges | | | | | | | | |
| Bitstamp | 0.203*** | 15.193 | 0.271*** | 15.533 | 0.248*** | 7.904 | 0.166*** | 7.849 |
| Coinbase | 0.195*** | 16.758 | 0.290*** | 18.503 | 0.206*** | 9.965 | 0.137*** | 5.893 |
| Gemini | 0.266*** | 13.145 | 0.310*** | 13.376 | 0.331*** | 7.750 | NA | NA |
| Panel B. Unregulated tier 1 exchanges | | | | | | | | |
| Binance | 0.354*** | 25.223 | 0.391*** | 35.160 | 0.393*** | 16.171 | 0.083*** | 3.529 |
| Bittrex | 0.096*** | 3.000 | 0.102*** | 2.898 | 0.114 | 1.691 | 0.137*** | 3.544 |
| Bitfinex | 0.221*** | 13.626 | 0.193*** | 12.202 | 0.236*** | 7.838 | 0.197*** | 6.004 |
| HitBTC | 0.039*** | 2.978 | 0.033*** | 3.572 | 0.039** | 2.086 | 0.035 | 1.602 |
| Huobi | 0.257*** | 24.010 | 0.147*** | 19.769 | 0.198*** | 10.850 | 0.059*** | 3.018 |
| KuCoin | −0.018 | −2.342 | 0.024 | 0.889 | 0.069 | 0.960 | −0.030 | −1.427 |
| Liquid | 0.185*** | 5.603 | 0.171*** | 4.938 | NA | NA | 0.247*** | 5.746 |
| Okex | 0.139*** | 16.418 | 0.105*** | 13.011 | 0.077*** | 5.647 | 0.035** | 2.012 |
| Poloniex | 0.163*** | 6.312 | 0.159*** | 7.099 | 0.239*** | 4.518 | 0.096*** | 2.768 |
| Zb | −0.010 | −2.025 | −0.009 | −6.041 | −0.029 | −3.679 | −0.013 | −7.457 |
| Panel C. Unregulated tier 2 exchanges | | | | | | | | |
| Bgogo | −0.008 | −45.062 | −0.014 | −2.571 | NA | NA | NA | NA |
| Biki | −0.007 | −18.615 | −0.002 | −0.596 | −0.009 | −10.838 | −0.009 | −12.036 |

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**Table 3.** (Continued)

Observation range: Multiples of 500 units (500× − 100, 500× + 100)

| | BTC/USD | | ETH/USD | | LTC/USD | | XRP/USD | |
|---|---|---|---|---|---|---|---|---|
| Exchange | Difference | $t$ statistics | Difference | $t$ statistics | Difference | $t$ statistics | Difference | $t$ statistics |
| BitZ | 0.007 | 1.122 | 0.041** | 2.366 | −0.055 | −1.133 | −0.070 | −0.843 |
| Coinbene | −0.005 | −3.509 | −0.001 | −0.142 | 0.006 | 0.451 | −0.001 | −0.096 |
| DragonEX | −0.009 | −3.261 | −0.014 | −4.028 | −0.006 | −3.890 | −0.006 | −8.531 |
| Lbank | −0.014 | −11.815 | −0.012 | −17.525 | NA | NA | NA | NA |
| Mxc | 0.079** | 2.078 | 0.246*** | 15.485 | 0.018* | 2.008 | −0.009 | −7.708 |
| Fcoin | 0.006 | 1.333 | 0.030*** | 3.498 | 0.000 | −0.022 | 0.003 | 0.415 |
| Exmo | 0.182** | 2.880 | 0.070 | 1.154 | NA | NA | 0.059 | 0.602 |
| Coinmex | −0.002 | −6.491 | −0.007 | −16.342 | NA | NA | NA | NA |
| Bibox | 0.369*** | 11.156 | 0.061*** | 9.883 | 0.062*** | 5.522 | −0.008 | −13.686 |
| Bitmart | −0.001 | −0.743 | −0.008 | −12.134 | −0.012 | −8.184 | NA | NA |
| Bitmax | 0.150*** | 5.935 | 0.098*** | 6.720 | 0.054*** | 2.845 | 0.155*** | 6.923 |
| Coinegg | −0.020 | −11.980 | −0.012 | −13.575 | −0.022 | −9.611 | 0.001 | 0.120 |
| Digifinex | −0.004 | −0.622 | −0.001 | −0.185 | −0.009 | −10.539 | −0.008 | −15.631 |
| Gateio | 0.219*** | 8.589 | 0.080*** | 4.489 | 0.051** | 2.499 | 0.036 | 1.442 |

*Notes.* In the table, two sets of $t$-test results with different testing points and observation windows are demonstrated: multiples of 100 units with a window radius 50 (100× − 50, 100× + 50), and multiples of 500 units with a window radius 100 (500× − 100, 500× + 100). A positive difference indicates that frequency at round size is higher than the rest within the observation window, that is, trade size clustering.

***, **, and * denote statistical significance levels at 1%, 5%, and 10%, respectively.

studies (Maslov and Mills 2001, Gabaix et al. 2006, Plerou and Stanley 2007) find that, in stock markets, trading volume distribution follows the power law with exponent $\alpha \cong 1.5$. For theory, Gabaix et al. (2006) propose a model derived from trading strategies by large institutional investors. Intuitively, institutional investors trade as much as possible, avoiding price impact to their robustness constraint. Given that fund sizes follow Zipf distribution, presumably from the random growth of funds, trade size conforms to the power law distribution with an exponent of 1/2. These conditions likely apply to cryptocurrency markets too; that is, cryptocurrency transaction sizes are highly likely to conform to a power law.

To examine trade size distribution tails, we use two widely adopted techniques: The first is to take the logarithm of the empirical probability density function and fit the log-log data to power law distribution by ordinary least squares (OLS). The second is to apply the maximum likelihood estimation (MLE) approach and use the Hill estimator $\hat{\alpha}_{Hill}$ for the data fitting. The Hill estimator is asymptotically normal and calculated as follows (Hill 1975, Clauset et al. 2009):

$$\hat{\alpha}_{Hill} = 1 + n\left(\sum_{i=1}^{n} ln\frac{x_i}{x_{min}}\right)^{-1}, \tag{5}$$

where $n$ is the number of observations and $x_{min}$ is the cutoff threshold. The distribution yields to power law after $x_{min}$. The cutoff $x_{min}$, which signifies the start of the tails, is set as the top 10% of the largest trades during the sampling period. In this study, trade size distributions are constructed for empirical probability density functions using logarithmic spacing, and the Python package "powerlaw" (Alstott et al. 2014) is applied to fit the data and calculate the exponent.

Gabaix et al. (2003b) show that, theoretically and empirically, stock trade size follows a half cubic law ($\alpha = 1.5$). Various studies on trading volumes or sizes show that the vast majority of tail exponents lie in the Pareto–Lévy regime ($1 < \alpha < 2$) for traditional financial assets and Bitcoins (Li et al. 2019, Schnaubelt et al. 2019).[18] We, thus, check whether the values of exponent $\alpha$ in the fitted results fall within the Pareto–Lévy range.

Table 4 presents the results from OLS and MLE fittings for four cryptocurrency trades. We can visually inspect the goodness of fit and identify whether crypto exchanges display a power law tail in trade size distribution as shown in Figure 4.

As anticipated, both scaling estimators $\hat{\alpha}_{OLS}$ and $\hat{\alpha}_{Hill}$ lie in the Pareto–Lévy regime on regulated exchanges, indicating a stable power law decay in all cryptocurrency transactions. Similar patterns are observed on half of the unregulated tier 1 exchanges. HitBTC and KuCoin have estimators that fall outside the Pareto–Lévy range for all cryptocurrencies, suggesting inconsistency with power law exponents for trade sizes in traditional markets. Furthermore, tail exponents for Liquid, Okex, and Zb display inconsistency for one cryptocurrency data.

On unregulated tier 2 exchanges, only three exchanges show estimated exponents within the Pareto–Lévy range, whereas 62.5% show statistical evidence of disconformity to parameters of empirical regularity in all cryptocurrencies. Among the remaining samples, Bitmart shows fitted exponents within the ranges for both LTC and ETH transactions. Coinegg displays a pattern

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**Table 4.** Power Law Fitting

| | BTC/USD | | | ETH/USD | | | LTC/USD | | | XRP/USD | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Exchange | $\hat{\alpha}_{OLS}$ | $\hat{\alpha}_{Hill}$ | Pareto–Lévy $(1<\alpha<2)$ | $\hat{\alpha}_{OLS}$ | $\hat{\alpha}_{Hill}$ | Pareto–Lévy $(1<\alpha<2)$ | $\hat{\alpha}_{OLS}$ | $\hat{\alpha}_{Hill}$ | Pareto–Lévy $(1<\alpha<2)$ | $\hat{\alpha}_{OLS}$ | $\hat{\alpha}_{Hill}$ | Pareto–Lévy $(1<\alpha<2)$ |
| Panel A. Regulated exchanges | | | | | | | | | | | | |
| Bitstamp | 1.806 | 1.279 | Y | 1.696 | 1.374 | Y | 1.510 | 1.849 | Y | 1.748 | 1.338 | Y |
| Coinbase | 1.763 | 1.191 | Y | 1.745 | 1.308 | Y | 1.857 | 1.309 | Y | 1.809 | 1.257 | Y |
| Gemini | 1.668 | 1.297 | Y | 1.762 | 1.425 | Y | 1.673 | 1.835 | Y | NA | NA | NA |
| Panel B. Unregulated tier 1 exchanges | | | | | | | | | | | | |
| Binance | 1.669 | 1.209 | Y | 1.795 | 1.436 | Y | 1.836 | 1.411 | Y | 1.960 | 1.430 | Y |
| Bittrex | 1.911 | 1.671 | Y | 1.582 | 1.880 | Y | 1.807 | 1.497 | Y | 1.798 | 1.722 | Y |
| Bitfinex | 1.680 | 1.277 | Y | 1.719 | 1.425 | Y | 1.815 | 1.397 | Y | 1.948 | 1.430 | Y |
| HitBTC | 0.620 | 0.663 | N | 0.785 | 0.790 | N | 0.692 | 0.879 | N | 0.552 | 0.803 | N |
| Huobi | 1.750 | 1.089 | Y | 1.842 | 1.505 | Y | 1.871 | 1.447 | Y | 1.966 | 1.651 | Y |
| KuCoin | 3.325 | 1.656 | N | 3.014 | 1.609 | N | 4.563 | 5.865 | N | 5.976 | 5.579 | N |
| Liquid | 1.406 | 0.905 | N | 1.494 | 1.358 | Y | NA | NA | NA | 1.282 | 1.231 | Y |
| Okex | 1.680 | 0.949 | N | 1.675 | 1.020 | Y | 1.863 | 1.320 | Y | 1.812 | 1.212 | Y |
| Poloniex | 1.629 | 1.008 | Y | 1.615 | 1.816 | Y | 1.662 | 1.428 | Y | 1.804 | 1.470 | Y |
| Zb | 1.479 | 1.095 | Y | 1.841 | 1.417 | Y | 1.546 | 0.932 | N | 1.634 | 1.194 | Y |
| Panel C. Unregulated tier 2 exchanges | | | | | | | | | | | | |
| Bgogo | 1.333 | 2.760 | N | 3.345 | 3.941 | N | NA | NA | NA | NA | NA | NA |
| Biki | 5.197 | 7.155 | N | 10.428 | 7.076 | N | 1.739 | 2.046 | N | 2.194 | 1.469 | N |
| BitZ | 2.374 | 2.702 | N | 2.035 | 1.546 | N | 2.014 | 4.005 | N | 2.202 | 4.452 | N |
| Coinbene | 4.546 | 2.724 | N | 4.716 | 3.573 | N | 7.165 | 4.137 | N | 6.356 | 4.157 | N |
| DragonEX | 2.269 | 1.701 | N | 4.367 | 1.773 | N | 0.641 | 1.299 | N | 8.689 | 4.863 | N |
| Lbank | 1.760 | 1.638 | Y | 1.998 | 1.622 | Y | NA | NA | NA | NA | NA | NA |
| Mxc | 7.660 | 7.063 | N | 3.598 | 11.444 | N | 14.815 | 11.706 | N | 12.439 | 6.862 | N |
| Fcoin | 1.020 | 0.952 | N | 1.157 | 0.874 | N | 1.241 | 0.765 | N | 0.656 | 0.650 | N |
| Exmo | 1.370 | 3.770 | N | 1.520 | 3.087 | N | NA | NA | NA | 1.486 | 6.373 | N |
| Coinmex | 4.292 | 7.578 | N | 7.384 | 7.966 | N | 5.049 | 8.802 | N | 10.697 | 13.863 | N |
| Bibox | 5.829 | 6.384 | N | 3.639 | 5.961 | N | 3.676 | 4.877 | N | 7.116 | 5.027 | N |
| Bitmart | 2.854 | 1.728 | N | 1.926 | 1.880 | Y | 1.572 | 1.226 | Y | 1.831 | 2.691 | N |
| Bitmax | 1.509 | 1.022 | Y | 1.669 | 1.191 | Y | 1.479 | 1.193 | Y | 1.434 | 1.180 | Y |
| Coinegg | 0.718 | 1.261 | N | 2.031 | 1.237 | N | 1.077 | 1.056 | Y | 6.551 | 10.524 | N |
| Digifinex | 1.537 | 1.038 | Y | 1.618 | 1.117 | Y | 1.679 | 1.129 | Y | 1.548 | 1.001 | Y |
| Gateio | 2.048 | 1.631 | N | 1.925 | 1.954 | Y | 2.173 | 2.430 | N | 2.175 | 2.074 | N |

*Notes.* This table shows the fitting results of the tails of trade size distribution. OLS and MLE are applied for the estimation of scaling parameters $\hat{\alpha}_{OLS}$ and $\hat{\alpha}_{Hill}$, respectively. We apply the probability density function to estimate the scaling exponents $1+\alpha$. We also check whether the estimated parameters are within the Pareto–Lévy range $(1<\alpha<2)$ and mark "Y" if both exponents lie within the Pareto–Lévy range.

consistent with the range for LTC, whereas Gateio does so for ETH.

Figure 4 displays the probability density for trade size and the fitted power law distributions on log-log plots with one regulated and four unregulated exchanges as representatives for brevity. Online Appendix F contains figures for the rest.

As in mainstream financial markets, transactions from regulated exchanges display a downward linear trend in log-log plots and appear visually fit with power law distributions. For instance, in panel Coinbase of Figure 4, empirical data points fall around the fitted lines without obvious outliers, implying that trades in regulated exchange generally follow power law in all four listed cryptocurrencies. In general, the OLS line fits equally in the whole range, whereas MLE estimation weighs more at the start of the tail, at which the probability value is higher. Consistent with regulated exchanges, 90% of unregulated tier 1 exchanges resemble power law tails in trade size distributions. Straight lines estimated by OLS and MLE are roughly fitted to the data. Conversely, KuCoin (shown in Figure 4) shows a curvy shape in tails and fails to show the power law distribution in the trade size.

On unregulated tier 2 exchanges, tail distributions exhibit a variety of behaviors and reveal irregular patterns across exchanges and cryptocurrencies. Four tier 2 exchanges (Lbank, Bitmax, Digifinex, Gateio) show a linear decrease in the tail zones and comply with the power law tail. Exmo (as shown in Figure 4) displays a good linear fit but is inconsistent with the MLE method. On Fcoin, data points are dispersed in the tails of BTC, ETH, and LTC trades; additionally, a curvy shape is observed on the logarithm scale in BTC and XRP trades. In Coinegg's BTC samples, the tail appears to be flat with some outliers. The ETH, LTC, and XRP graphs of Coinegg show step-like decay patterns.

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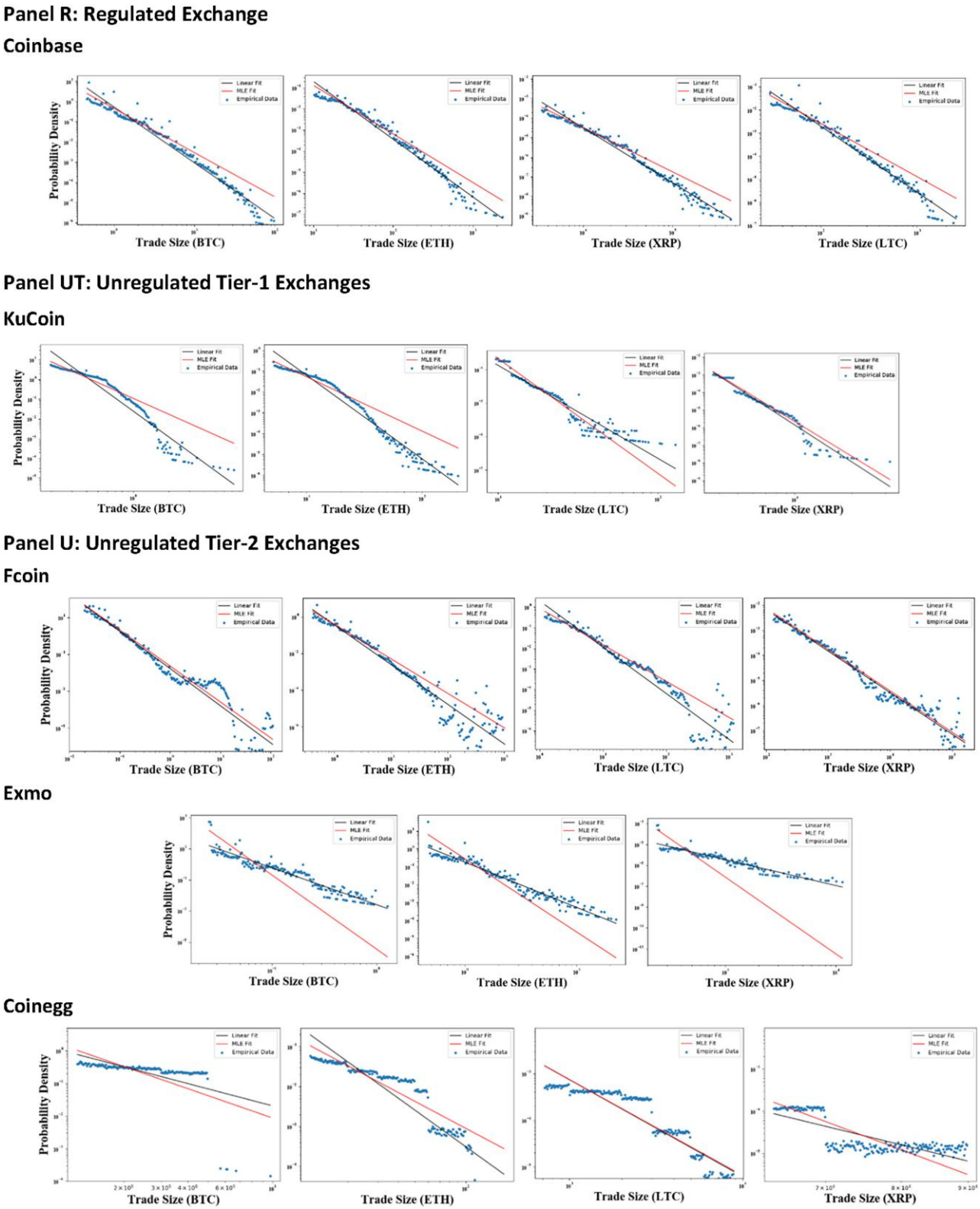
**Figure 4.** (Color online) Tail Distribution and Power Law Fitting




*Notes.* This figure displays the tails of trade size distributions and the fitted power law lines on log-log plots. The fitted power law lines are plotted with parameters estimated by OLS and MLE. The dots represent empirical data points for trade size frequencies.

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The findings suggest that regulated exchanges behave as power law predicts with estimators consistent with the Pareto–Lévy exponents in mainstream financial markets. But only half of tier 1 exchanges display a power law tail with exponents characterized by the Pareto–Lévy regime in all cryptocurrencies. In contrast, 75% of tier 2 exchanges fail to follow.

### 3.4. Selection Concern, Multihypothesis Testing, and Conclusive Evidence

So far, we have conducted three independent statistical analyses for each cryptocurrency on every crypto exchange, including the chi-squared test for Benford's law distribution, the *t*-test for trade-size clustering, and the linear fit for power law. The results are consistent for each category (regulated, unregulated tier 1, and tier 2) and for most exchanges. Overall, more than half of the unregulated exchanges fail at least half of all tests at the 5% significance level. Except for Bitmax, tier 2 exchanges fail at least 30% of the tests with 10 exchanges failing more than 65% of all the tests. At the cryptocurrency level, unregulated exchanges as a whole fail more than 40% of the tests for each cryptocurrency. In contrast, regulated exchanges pass all the tests. These findings align with prediction 1 of the theoretical model (Online Appendix G), indicating that exchanges under regulations are less likely to engage in wash trading than those without regulation. Furthermore, consistent with prediction 2, companies in jurisdictions with higher fines (i.e., the United States) are less likely to wash trade compared with ones with a lower level of fine (i.e., Japan). Notably, the United States is a major country that regularly establishes enforcement actions and issues fines against cryptocurrency exchanges (Blandin et al. 2019, Robinson 2021).

Because multiple statistical tests may increase the possibility of type I error and raise the concern of *p*-hacking, we perform a multiple (global) hypothesis test for robustness. The details and the results of the test can be found in Online Appendix H. The results are consistent with our findings in previous sections. Trade patterns of all regulated exchanges show insignificant differences from those of traditional financial markets. Tier 1 unregulated exchanges have lower proportions in rejecting null hypotheses than tier 2 ones in all cryptocurrencies. Seventy-five percent of the tier 2 unregulated exchanges fail to follow the universal law or trade patterns of traditional financial markets. In addition, BTC has the highest failure rates, followed by XRP. Furthermore, more unregulated exchanges fail the joint tests than individual tests in all cryptocurrency pairs. Some fraudulent exchanges may "luckily" display similar trade distribution as traditional markets in certain aspects but fail to satisfy all regularities, therefore leading to higher failed percentages in multiple hypothesis tests.

We also advocate combining the various detection approaches because every exchange may engage in wash trading differently, and just because of randomness, an individual test may contain type I and II errors. For example, Aloosh and Li (2023) find that using power law tail distribution does not detect wash trading on Mt. Gox during an earlier episode. This does not invalidate the approach and may be explained by the fact that, in the early days, wash trades are characterized by a large quantity of small transactions as the authors document or the high volatility of Bitcoin prices.

One might be concerned that traders and algorithms are unique or self-selected on unregulated exchanges. However, it is documented that trading algorithms are generally exchange agnostic (Alameda 2019). Furthermore, according to PwC (2022), institutional investors choose trading venues primarily based on exchange liquidity and opportunities rather than their regulatory status. We find no significant difference regarding the volume and distribution of transactions on regulated exchanges compared with unregulated exchanges when they became regulated. For example, Coinbase received its BitLicense in 2017 with no exodus of traders. In fact, its trading volume increased significantly since.

Whereas these may not completely rule out traders' self-selecting into trading on regulated versus unregulated exchanges, we further appeal to the power of Benford's law and power law to allay our concern. If institutional investors or algorithmic traders systematically prefer regulated or unregulated exchanges, it would bias our findings toward seeing different tail distributions and less rounding on those exchanges. However, power law distributions for the tail can have different cutoffs, so having disproportionally large trades is unlikely to affect the general shape of the tail (it could affect the exponent parameter). Moreover, whether one transacts large amounts or uses algorithms should not affect the first significant digit distribution because Benford's law is robust to changing accounting units and rounding behavior. Therefore, the three tests complement one another.

## 4. Quantifying Wash Trading

We now quantify the extent of wash trading by directly estimating wash trading volume. We also conduct several robustness and validation tests and provide alternative wash trading metrics.

### 4.1. Trade-Size Roundness and Benchmark Roundness Ratio

Authentic human trades tend to have round sizes. In contrast, unrounded trades typically relate to programmed trading for various purposes, such as market marking, high-frequency arbitration, and in particular wash trading. Strong evidence suggests that most wash trading is done by bots, which can be easily added to the trading structure

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scripted by simple Python programs (e.g., Vigna and Osipovich 2018, Rodgers 2019), making round/unrounded trades reasonable proxies for authentic/fake orders.

We first show that levels of roundness for trade sizes differ across unregulated and regulated exchanges. The level of roundness is a qualitative parameter describing the decimal or integer places of the last nonzero digit. For instance, 1.01 BTC has a higher level of roundness than 2.123 BTC; 100 ETH has a higher level of roundness than 1,234 ETH.[19] Authentic trades should display a higher level of roundness in size than artificial ones. We, thus, expect regulated exchanges to present a higher level of roundness in trade sizes compared with unregulated exchanges. For each crypto exchange, we analyze the trade size distribution over levels of roundness (ten thousands, thousands, hundreds, tens, ones, tenths, hundredths, etc. base units). We then compare the regulated versus unregulated exchanges.

Table 5 shows that tier 1 exchanges have significantly large chi-squared statistics in at least one cryptocurrency. Unregulated tier 2 exchanges, except for Mxc in BTC trades, show different roundness distributions from regulated exchanges with a 1% significance level for nearly all cryptocurrencies. Evidently, unregulated exchanges, especially unregulated tier 2 exchanges, have a lower level of roundness in trade size relative to the regulated exchanges.

Assuming that the computer-based, legitimate (non-wash) trades on unregulated exchanges have the same sensitivity to the authentic trading strategies and exchange characteristics as those on regulated exchanges, we estimate the legitimate number of unrounded trades for unregulated exchanges. The difference between the observed unrounded and legitimate trading volume is then a reasonable proxy for wash-trading volume. Because one can rarely label wash trades at an exchange without detailed information about the traders, our method provides a general way of estimating systematic wash trading that can be time-varying, therefore serving as a first order benchmark.

From our earlier analysis, we detect no systematic wash trading on regulated exchanges. This is corroborated by

**Table 5.** Chi-Squared Test for Trade Size Roundness of Unregulated Exchanges

| | BTC/USD | | ETH/USD | | LTC/USD | | XRP/USD | |
|---|---|---|---|---|---|---|---|---|
| Exchange | $\chi^2$ | $p$-value | $\chi^2$ | $p$-value | $\chi^2$ | $p$-value | $\chi^2$ | $p$-value |
| Panel A. Unregulated tier 1 exchanges | | | | | | | | |
| Binance | 9.545 | 0.145 | 15.013** | 0.020 | 12.18** | 0.032 | 11.993*** | 0.007 |
| Bittrex | 3.100 | 0.796 | 11.455* | 0.075 | 9.222 | 0.101 | 13.387*** | 0.004 |
| Bitfinex | 92.104*** | 0.000 | 8.086 | 0.232 | 5.616 | 0.345 | 51.094*** | 0.000 |
| HitBTC | 17.224*** | 0.008 | 13.387** | 0.037 | 7.547 | 0.183 | 11.393*** | 0.010 |
| Huobi | 115.48*** | 0.000 | 11.01* | 0.088 | 14.311** | 0.014 | 9.5** | 0.023 |
| KuCoin | 7.909 | 0.245 | 17.469*** | 0.008 | 24.886*** | 0.000 | 16.603*** | 0.001 |
| Liquid | 182.435*** | 0.000 | 16.518** | 0.011 | NA | NA | 49.766*** | 0.000 |
| Okex | 4.384 | 0.625 | 15.649** | 0.016 | 19.46*** | 0.002 | 12.18*** | 0.007 |
| Poloniex | 3.247 | 0.777 | 5.427 | 0.490 | 11.906** | 0.036 | 14.268*** | 0.003 |
| Zb | 1,461.8*** | 0.000 | 692.292*** | 0.000 | 21.797*** | 0.001 | 18.032*** | 0.000 |
| Panel B. Unregulated tier 2 exchanges | | | | | | | | |
| Bgogo | 18.774*** | 0.005 | 32.402*** | 0.000 | NA | NA | NA | NA |
| Biki | 60.923*** | 0.000 | 62.726*** | 0.000 | 28.101*** | 0.000 | 19.651*** | 0.000 |
| BitZ | 828.828*** | 0.000 | 85.86*** | 0.000 | 22.242*** | 0.000 | 19.593*** | 0.000 |
| Coinbene | 1,670.819*** | 0.000 | 31.158*** | 0.000 | 32.097*** | 0.000 | 19.747*** | 0.000 |
| DragonEX | 1,668.236*** | 0.000 | 20.761*** | 0.002 | 27.753*** | 0.000 | 19.109*** | 0.000 |
| Lbank | 1,639.493*** | 0.000 | 24.944*** | 0.000 | NA | NA | NA | NA |
| Mxc | 9.569 | 0.144 | 15.481** | 0.017 | 18.705*** | 0.002 | 19.688*** | 0.000 |
| Fcoin | 740.835*** | 0.000 | 157.443*** | 0.000 | 86.741*** | 0.000 | 18.59*** | 0.000 |
| Exmo | 15.455** | 0.017 | 26.838*** | 0.000 | NA | NA | 19.182*** | 0.000 |
| Coinmex | 1,719.65*** | 0.000 | 23.694*** | 0.001 | 32.242*** | 0.000 | 19.796*** | 0.000 |
| Bibox | 439.322*** | 0.000 | 101.26*** | 0.000 | 14.106** | 0.015 | 19.458*** | 0.000 |
| Bitmart | 18.605*** | 0.005 | 28.754*** | 0.000 | 22.785*** | 0.000 | 19.768*** | 0.000 |
| Bitmax | 26.08*** | 0.000 | 130.687*** | 0.000 | 41.623*** | 0.000 | 34.596*** | 0.000 |
| Coinegg | 1,310.242*** | 0.000 | 34.176*** | 0.000 | 30.144*** | 0.000 | 19.728*** | 0.000 |
| Digifinex | 1,546.727*** | 0.000 | 23.247*** | 0.001 | 29.609*** | 0.000 | 19.592*** | 0.000 |
| Gateio | 535.379*** | 0.000 | 55.367*** | 0.000 | 13.247** | 0.021 | 15.288*** | 0.002 |

*Notes.* This table presents the results of Pearson's chi-squared test on the roundness of unregulated exchanges with regulated exchanges as a benchmark. Results of unregulated tier 1 and 2 exchanges are shown in panels A and B, respectively. The level of roundness is a parameter describing the decimal or integer places of the last nonzero digit. Test results, $\chi^2$ statistics and $p$-values, reveal the difference in distributions between regulated and unregulated exchanges.

***, **, and * denote the statistical significance levels at 1%, 5%, and 10%, respectively.

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the fact that round trades constitute around 30% of total trades on regulated crypto exchanges, which is consistent with patterns in the U.S. equity markets that are approximately free of wash trading because of regulation (Gomber et al. 2009, Tabb et al. 2009). We carry out a cross-validation test using any two regulated exchanges as the no wash trading benchmark to estimate the wash-trading amount on the remaining regulated exchange. We find the wash trades estimated, on average, constitute less than 5% of the reported volumes.

### 4.2. Estimated Volume of Wash Trades

We estimate the wash-trading volume by calculating the abnormal proportion of unrounded trades. Specifically, we categorize trading volumes into round and unrounded ones by checking if the last nonzero digit of a certain trade size is less than 100 basis units. We then perform a pooled regression to estimate the ratio of (log) unrounded volume to (log) round volume at a weekly frequency:

$$\ln(V_{Unrounded_{it}}) = \alpha + \beta * \ln(V_{Round_{it}}) + \gamma * \boldsymbol{X_{it}} + \epsilon_{it}, \quad (6)$$

where $V_{Unrounded_{it}}$ and $V_{Round_{it}}$ are unrounded and round trading volumes of regulated exchange $i$ at week $t$, respectively. In the baseline, we exclude exchange-level controls by setting $X_{it}$ to zero. To mitigate the concern that heterogeneous authentic algorithmic trading on various exchanges drives the estimates, we include a vector of exchange characteristics, $\boldsymbol{X_{it}}$, including age, rank, CoinMarketCap web traffic percentage, and unique visitors, in an alternative specification. We employ the parameters in (6) to calculate the legitimate (nonwash) unrounded trades of unregulated exchanges using their corresponding round trades. Wash trade volume is, thus, calculated as the nonnegative amount by which the total unrounded trades exceed legitimate unrounded trades.

Table 6 presents the simple averaged and volume-weighted wash-trading percentage for each exchange category and the exchange-level wash-trading percentage by four cryptocurrency pairs. The results using models with or without controls are similar. Because some exchanges have missing data on the control variables and the residual standard errors in the model without controls are comparable to those with controls (meaning out-of-sample predictability is comparable), we only report the results using estimates from the model without controls for simplicity in subsequent analyses on price impacts, ranking, and so on. Standard deviations of wash-trading volumes from bootstrapping the sample 1,000 times are also included in the table.

On average, wash trades account for more than 70% of the total trading volume on each unregulated exchange and approximately 61% even after controlling for exchange characteristics. Wash trades represent 53.4% of tier 1 and 81.7% of tier 2 exchanges' volume. Given that the four cryptocurrencies we examine dominate transaction volumes on all the exchanges, these figures are informative even without including all cryptocurrencies. It is also noteworthy that, for all unregulated exchanges, an estimated 77.5% of the total reported volume appears to be wash trades. Our estimates are in the same order of magnitude as the estimates from *The Wall Street Journal* and industry reports (Blockchain Transparency Institute 2019, Rodgers 2019), which are in the range of 67%–99%. For example, the Blockchain Transparency Institute Summary of Market Surveillance report discovered that, as of April 2019, 17 of the top 25 exchanges listed on CoinMarketCap contained more than 99% fake volume. Our estimates are lower because exchanges might have taken actions since those earlier estimates were published—the Lucas critique applies.

### 4.3. Further Validation and Robustness Tests

Some may be concerned that heterogenous traders and, thus, their strategies across crypto exchanges could distort our estimation of wash trade. To alleviate the concerns, we use Benford's law and power law to test if our estimation (Section 4.2) predominantly captures wash trading. The results in Online Appendix I indicate the roundness-based estimation to be unaffected by authentic algorithmic trades.

That said, we provide complementary metrics that should help convince the readers that wash trading on unregulated exchanges is rampant and economically significant. One shows the extent of an exchange's wash trading by summarizing results of statistical tests in Section 4, grouped by exchanges and cryptocurrencies separately. Details can be found in Online Appendix J. In addition, we compare the trade size distribution of unregulated exchanges to regulated exchanges for robustness (Online Appendix K). Then, we examine an alternative method to gauge the extent of wash trading using Benford's law in Online Appendix L. Finally, we discuss existing industry reports and why our methodologies are likely to be more robust and superior in Online Appendix M.

## 5. Wash Trading Incentives, Impacts, and Implications

We now discuss the potential drivers and implications of crypto wash trading, starting with the incentives for wash trading and how it affects the ranking of crypto exchanges. We then analyze the characteristics of exchanges that portend wash trading and explore wash trading's impacts on crypto asset prices before examining its regulatory and industrial ramifications.

In traditional markets, wash trading is typically conducted by individual traders rather than platforms. However, individual wash traders alone cannot fully explain the differences observed between regulated and unregulated exchanges. Whereas the cost of wash trading for individuals should be associated with fees and bid–ask spreads, there is no systematic correlation found

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**Table 6.** Estimating the Fraction of Wash Trades

Panel A. Aggregated wash trading percentage

| | Wash trade percentage without control variables | | Wash trade percentage with control variables | |
|---|---|---|---|---|
| | Equal-weighted average | Volume-weighted average | Equal-weighted average | Volume-weighted average |
| Unregulated | 70.85 | 77.50 | 60.96 | 71.43 |
| Unregulated tier 1 | 53.41 | 61.86 | 46.95 | 63.62 |
| Unregulated tier 2 | 81.76 | 86.26 | 70.96 | 76.96 |

Panel B. Wash trading percentage for unregulated tier 1 exchanges

| Exchange | Wash trade percentage no control | Wash trade percentage with control |
|---|---|---|
| Binance | 51.76 (1.28) | 46.47 (1.34) |
| Bittrex | 51.73 (1.65) | 18.91 (2.34) |
| Bitfinex | 1.87 (0.52) | 31.34 (2.06) |
| HitBTC | 92.60 (0.66) | 89.81 (1.93) |
| Huobi | 44.87 (2.08) | 57.77 (1.69) |
| KuCoin | 74.36 (1.30) | 52.96 (6.67) |
| Liquid | 19.02 (1.55) | 3.02 (1.41) |
| Okex | 66.12 (1.52) | 72.75 (2.02) |
| Poloniex | 37.49 (2.46) | 14.94 (2.19) |
| Zb | 94.31 (0.54) | 81.49 (4.20) |

Panel C. Wash trading percentage for unregulated tier 2 exchanges

| Exchange | Wash trade percentage no control | Wash trade percentage with control |
|---|---|---|
| Bgogo | 99.99 (0.00) | 99.93 (0.01) |
| Biki | 99.36 (0.13) | NA |
| BitZ | 72.72 (2.41) | 72.62 (2.18) |
| Coinbene | 95.50 (0.52) | 91.64 (1.51) |
| DragonEX | 89.71 (0.39) | 72.48 (2.55) |
| Lbank | 98.13 (0.21) | 98.65 (0.11) |
| Mxc | 82.00 (3.68) | NA |
| Fcoin | 77.09 (2.17) | 48.62 (5.32) |
| Exmo | 81.12 (4.21) | 64.99 (3.85) |
| Coinmex | 98.45 (0.09) | 86.12 (2.27) |
| Bibox | 34.32 (6.57) | 33.63 (5.75) |
| Bitmart | 98.10 (1.07) | 94.79 (2.04) |
| Bitmax | 65.42 (2.12) | 61.71 (2.21) |
| Coinegg | 96.80 (1.10) | 81.24 (3.18) |
| Digifinex | 94.36 (0.48) | 68.66 (5.38) |
| Gateio | 25.04 (4.49) | 18.42 (4.47) |

*Notes.* This table reports the pooled regression results of the fraction of wash trading for unregulated exchanges. The regression equation specifies the relationship between round and unrounded trade volumes:

$$\ln(V_{Unrounded_{it}}) = \alpha + \beta * \ln(V_{Round_{it}}) + \gamma * \boldsymbol{X_{it}} + \epsilon_{it},$$

where $\ln(V_{Round\,it})$ and $\ln(V_{Unrounded\,it})$ are the logarithms of round trade volume and unrounded trade volume, respectively, for exchange $i$ at week $t$; $\boldsymbol{X_{it}}$ is a vector of exchange characteristics, and $\epsilon_{it}$ is an error term. We categorize trading volume into round and unrounded ones by checking if the mantissa of a particular transaction volume is less than 100 base units or not. Exchange characteristics such as age, rank, CoinMarketCap web traffic percentage, and unique visitors are used as control variables. Exchange Biki and Mxc do not have data on control variables. The regression coefficients are used as a benchmark to calculate the expected unrounded trading volume, then the fraction of wash trading for each unregulated exchange. Fractions of wash trading are estimated for each cryptocurrency of each exchange (panels B and C for unregulated tier 1 and 2 exchanges, respectively) and then the aggregated amount (panel A) using equal- and volume-weighted averages. A thousand bootstrapped samples are used to calculate the standard deviation of wash trading estimates, which we report in brackets.

between the extent of wash trading and these variables. In contrast, evidence abounds that exchanges wash trade either directly or indirectly. For instance, top executives at some exchanges are known to trade on their own platforms and manage cryptocurrency hedge funds (e.g., Bitfinex'ed 2017). Additionally, multiple companies have also pleaded guilty to direct wash trading (Sinclair 2020). Moreover, exchanges can facilitate wash trading indirectly through fee rebate programs that incentivize their customers to engage in such activities. For example, Fcoin rewards platform tokens for trade mining, by which more FT tokens are earned by trading more.

### 5.1. Wash Trading and Exchange Ranking

Exchanges' profit crucially depends on brand awareness and website traffic for customer acquisition, both of

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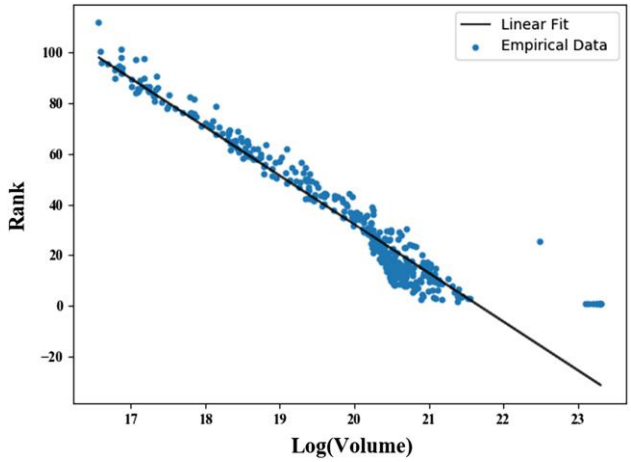
which heavily rely on public rankings. We utilize the proprietary, high-frequency data on exchange ranks and reported trading volumes from CoinMarketCap.com, on which most exchanges rely for referral traffic.[20] To study the incentives for wash trading by crypto exchanges, we first verify the ranking rule of CoinMarketCap using the daily rankings and reported volumes of more than 260 crypto exchanges. The Spearman rank order correlation coefficient is estimated to measure the rank correlation between trade volume and ranking in the CoinMarketCap. The coefficient is −0.995, approaching −1, indicating that ranks and volume are perfectly negatively related (see Figure 5). The rankings of CoinMarketCap are determined by the trade volume of crypto exchanges. Exchanges with larger volumes would rank higher and gain more visibility and visits.

Our findings support the intuition that, to survive the fierce competition, many crypto exchanges naturally wash trade to gain prominence and market share so that the exchange can generate higher profits.[21] Indeed, from Figure 6, we observe that a 70% wash trading volume can move the rank of an exchange up by more than 25 positions relative to its rank in a world without wash trading.

## 5.2. Price Impacts of Wash Trading

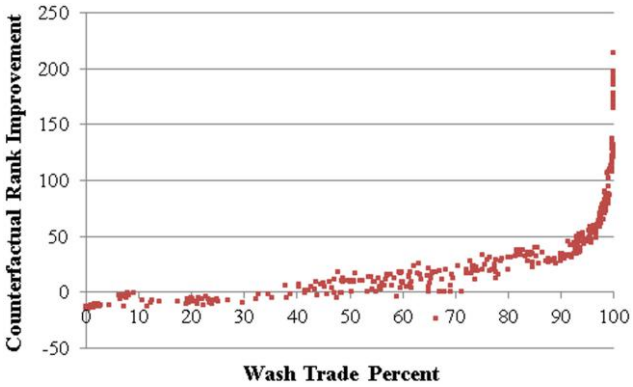
In Table 7, we examine the effect of wash trading on cryptocurrency prices. Panel A illustrates the relationship between wash-trading volumes and weekly returns. Panel B further reports whether wash trading makes the price listed on unregulated exchanges deviate from "fair" prices on regulated exchanges. For each unregulated exchange, price deviation is measured as the log difference between its weekly close price and the average

**Figure 5.** (Color online) Trading Volumes and Ranks




*Notes.* This figure plots the quantitative relationship between (logarithm) trade volumes and exchange ranks. Data fitting is carried out with OLS regression. The estimated coefficients are reported below ($t$-statistics in brackets) with an adjusted $R^2$ of 93%: Exchange rank$_i$ = $416.269 - 19.202 * \log(\text{Volume}_i) + \varepsilon_i$.

**Figure 6.** (Color online) Improvement in Ranks and Wash Trading




*Notes.* This figure plots the relationship between the estimated fraction of wash trading and the improvement in counterfactual ranks. The counterfactual rank is estimated based on the estimated real volume for any specific exchange, that is, the difference between the reported volume in CoinMarketCap and the estimated wash trading volume, using the volume–rank relationship documented in Figure 5. Rank improvement is the difference between the counterfactual rank and the reported rank in CoinMarketCap.

price from regulated exchanges (whose prices are very similar). In both panels, we regress these price indicators on logarithms of estimated wash trade volumes and control for features of exchanges in both contemporaneous and predictive regression specifications. The random effect model is adopted in all regressions based on the Hausman test with robust standard errors clustered at the exchange–currency level. We also include the currency fixed effect as robustness in both panels.

As shown in panel A of Table 7, wash-trade volume exhibits a positive and significant correlation with the weekly return in the same week. This result supports prediction 4 as outlined in our theoretical model (Online Appendix G), which posits that wash trading is proportional to cryptocurrency prices. However, this relation reverses in the following week. The coefficients are statistically and economically significant as shown in Models 3 and 7 of Table 7, panel A). A one standard deviation increase in wash trade volume(log) leads to a 0.63% increase in concurrent weekly return (annualized 32.76%), followed by a 0.42% decrease in the subsequent week (annualized 21.8%). The reverse relation with return suggests that higher wash-trade volume drives up the contemporaneous price, but the wash-trade effect on price does not last long, and the price reverses in the following week. What we observe is intuitive: faking transactions at higher prices can attract more investors who like to chase returns, but arbitrageurs close the pricing gap across exchanges over the next week.

To substantiate this intuition, we treat prices on regulated exchanges as fair price benchmarks and examine the price deviation of unregulated exchanges against this benchmark. Panel B shows a strong and positive

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**Table 7.** Price Impacts of Wash Trading

Panel A. Returns and wash trading

| | Weekly return$_t$ | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) |
| (log) wash trade volume$_t$ | 0.001*** | 0.001 | 0.003*** | 0.002*** | | | | | 0.024*** | 0.023*** | 0.024*** | 0.023*** |
| | (2.61) | (1.33) | (3.11) | (2.96) | | | | | (4.75) | (4.68) | (4.66) | (4.61) |
| (log) wash trade volume$_{t-1}$ | | | | | −0.001*** | −0.002*** | −0.002*** | −0.003*** | −0.024*** | −0.024*** | −0.024*** | −0.024*** |
| | | | | | (−2.95) | (−4.80) | (−3.37) | (−4.48) | (−4.83) | (−4.83) | (−4.70) | (−4.71) |
| Exchange age$_t$ | | | −0.000 | 0.000 | | | −0.000 | −0.000 | | | 0.000 | 0.000 |
| | | | (−0.07) | (0.17) | | | (−0.29) | (−0.34) | | | (0.02) | (0.50) |
| Tier 1 exchange | | | 0.001 | −0.000 | | | 0.005 | 0.004 | | | 0.001 | −0.001 |
| | | | (0.29) | (−0.12) | | | (1.46) | (1.56) | | | (0.33) | (−0.41) |
| (log) number of unique visitors | | | −0.000 | 0.000 | | | −0.001 | −0.001 | | | −0.000 | 0.000 |
| | | | (−0.30) | (0.28) | | | (−1.15) | (−1.25) | | | (−0.26) | (0.71) |
| CMC rank$_t$ | | | 0.000*** | 0.000*** | | | −0.000 | −0.000** | | | 0.000 | 0.000 |
| | | | (3.23) | (3.68) | | | (−1.24) | (−2.09) | | | (1.24) | (1.32) |
| Constant | −0.049*** | −0.027*** | −0.080*** | −0.070*** | 0.010 | 0.030*** | 0.037** | 0.067*** | −0.008 | 0.010 | −0.016 | −0.003 |
| | (−5.15) | (−3.11) | (−3.35) | (−3.60) | (1.28) | (3.49) | (2.26) | (3.50) | (−1.14) | (1.46) | (−0.93) | (−0.23) |
| Currency fixed effects | N | Y | N | Y | N | Y | N | Y | N | Y | N | Y |
| Observations | 1,416 | 1,416 | 1,328 | 1,328 | 1,326 | 1,326 | 1,246 | 1,246 | 1,305 | 1,305 | 1,225 | 1,225 |
| Overall $R^2$, % | 0.1 | 1.0 | 0.4 | 1.2 | 0.1 | 1.1 | 0.2 | 1.2 | 3.1 | 4.0 | 3.3 | 4.1 |

Panel B. Price deviations and wash trading

| | PriceDeviation$_t$ | | PriceDeviation$_{t+1}$ − PriceDeviation$_t$ | |
|---|---|---|---|---|
| | (1) | (2) | (3) | (4) |
| (log) wash trade volume$_t$ | 0.046*** | 0.040*** | −0.048*** | −0.051*** |
| | (3.33) | (2.59) | (−3.97) | (−3.31) |
| Exchange age$_t$ | −0.000 | −0.000 | 0.000 | 0.000 |
| | (−0.19) | (−0.00) | (0.96) | (0.89) |
| Tier 1 exchange | 0.095 | 0.080 | −0.160 | −0.155 |
| | (1.25) | (1.12) | (−1.55) | (−1.47) |
| (log) number of unique visitors | −0.021 | −0.017 | 0.020 | 0.020 |
| | (−1.15) | (−1.10) | (1.08) | (1.01) |
| CMC rank$_t$ | 0.005*** | 0.005*** | −0.004*** | −0.004*** |
| | (4.60) | (4.16) | (−3.55) | (−3.17) |
| Constant | −1.112*** | −0.968** | 1.080*** | 1.147** |
| | (−3.01) | (−2.35) | (3.02) | (2.50) |
| Currency fixed effects | N | Y | N | Y |
| Observations | 1,328 | 1,328 | 1,246 | 1,246 |
| Overall $R^2$, % | 0.7 | 1.1 | 0.4 | 0.5 |

*Notes.* This table presents the results of the regression analysis. In panel A, the dependent variable is the weekly returns for every cryptocurrency on every exchange. In panel B, the price deviation is calculated as the (log) difference between the close price of each unregulated exchange and averaged close prices of regulated exchanges at the same time. In both panels, wash trading volume is calculated as weekly wash trading percentage times volume. Exchange age$_t$ is the time span from its establishment to week $t$ for an exchange. Tier 1 exchange is a dummy variable that equals one if the exchange is an unregulated tier 1 exchange and zero otherwise. The number of unique visitors refers to the number of distinct visitors recorded during the sample period derived from SimilarWeb August to October 2019 reports. CoinMarketCapRank$_t$ is the rank directly obtained from CoinMarketCap. All models are estimated with random effects based on the Hausman test. Currency fixed effects are included in Models 2, 4, 6, 8, 10, and 12 of panel A and Models 2 and 4 of panel B. Standard errors are clustered at the exchange-currency level. $t$-statistics are reported in the brackets.

***, **, and * denote the statistical significance levels at 1%, 5%, and 10%, respectively.

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relationship between wash-trading volume and price deviations, controlling exchange characteristics. Considering the average wash-trade percentage of 70% for unregulated exchanges, such an increase in wash trade volume leads to a 3.22% higher price on unregulated exchanges compared with their regulated counterparts, reflecting its significant economic implications. This finding also corresponds to prediction 4. In addition, the price deviation converges to a marginal difference of 0.014% in the following period (as shown in Models 1 and 3 of Table 7, panel B). This observation aligns with the idea that arbitrageurs take advantage of price differences across various exchanges in the following week, thereby reducing price deviations.

### 5.3. Determinants of Wash Trading

We first investigate which types of exchanges are more likely to engage in wash trading. We run a cross-sectional regression of the overall fraction of wash trades on an exchange against its characteristics as shown in Table 8. Robust standard errors are calculated to tackle heteroskedasticity. In the regressions, we include the age of the exchange and all three traffic indicators derived from a series of SimilarWeb reports. The number of unique visitors refers to the number of distinct individuals visiting a web page, which is a close indicator of the user number or the "real" traders in the exchanges. A smaller number also implies that more visitors may have accessed the exchanges through third-party aggregators or referrals of the ranking websites. The other two indicators are based on each exchange's top five traffic geographical origins. We rank all traffic countries based on gross domestic product (GDP) and financial access.[22] The number of countries ranked in the bottom 15 is counted if they appear in the top five traffic countries for crypto exchange.

Table 8 demonstrates that the number of unique visitors is negatively correlated with wash trading, suggesting that exchanges with fewer unique visitors have a higher proportion of wash trades. From a *t*-test grouped by number of unique visitors, platforms with more than 100,000 unique users on average engage in wash trading for 60.21% of the reported volume, which is significantly less than 82.69% for those with fewer than 100,000 users. These results align with the economic incentives behind wash trading. The prevailing notion among practitioners is that exchanges with a larger number of real users are subject to greater scrutiny, leading to stronger reputational concerns and a motivation to maintain transparency and accuracy (Rodgers 2019). This observation is also following prediction 3 outlined in our theoretical framework.

In addition, we observe a negative relationship between the age of exchange and the fraction of wash trades, statistically significant at a 1% level. The adjusted $R^2$ is 28.4% in Model 1, implying that the age of exchange is one leading factor correlated with the decision to wash trade. Newly established exchanges are more eager to wash trade because it is a shortcut to increase brand awareness and acquire clients. In fact, unregulated exchanges more than five years old, on average, wash trade 47.83% of the

**Table 8.** Wash Trading and Exchange Characteristics

| | Unregulated exchange | | |
|---|---|---|---|
| Fraction of wash trades | (1) | (2) | (3) |
| Exchange age | −0.660*** | | −0.679*** |
| | (−2.99) | | (−3.08) |
| Number of unique visitors | | −0.099** | −0.091*** |
| | | (−2.12) | (−3.69) |
| Top 5 traffics from lower GDP countries | | | 3.152 |
| | | | (0.65) |
| Top 5 traffics from worst financial access countries | | | 4.956 |
| | | | (0.92) |
| Constant | 94.500*** | 72.995*** | 87.263*** |
| | (11.53) | (11.69) | (8.10) |
| Observations | 26 | 26 | 26 |
| Adjusted $R^2$, % | 28.4 | 1.0 | 30.1 |

*Notes.* This table reports the cross-sectional regression analysis for the relationship between the fraction of overall wash trading volume for an exchange and its characteristics. Exchange age is the span between the establishment date and July 2019, the start of our sample period. The remaining indicators are derived from SimilarWeb August to October 2019 reports. The number of unique visitors refers to the number of distinct visitors recorded during the sampling period. Top 5 traffics from lower GDP countries refers to the number of traffic countries ranked at the bottom 15 countries based on GDP. Top 5 traffics from worst financial access countries denotes the number of traffic countries ranked at the bottom 15 countries based on financial access. GDP and financial access data are obtained from the World Bank DataBank. The rank of countries is based on the average value of GDP and financial access over three years from 2016 to 2018. Robust standard errors are calculated. *t*-statistics are reported in the brackets.

***, **, and * denote the statistical significance levels at 1%, 5%, and 10%, respectively.

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reported volume, a significantly lower percentage compared with 81.32% for exchanges with less than five years.

The insignificant relationship with traffic country indicators implies that the extent of exchanges' wash trading may not vary across countries. We expect exchanges that rely more on referral traffic to have more incentives for wash trading, but this does not show up in our data because of either the short sampling period or the fact that many exchanges may not actively monitor web traffic sources.

Next, we investigate how market dynamics affect wash trading. Table 9 presents a panel regression of wash trade volumes on lagged "true" cryptocurrency weekly return and volatility obtained from the third-party composite price index on CoinMarketCap.[23] Standard errors are clustered at an exchange–currency level.

In Table 9, lagged cryptocurrency returns positively predict wash trade volume, whereas lagged volatility shows a strong negative prediction. In other words, misbehaving crypto exchanges tend to increase wash trading volumes when the market experiences recent positive returns or decreases in volatility in the past one or two weeks. Price increases could draw retail investors' attention and encourage speculation. Therefore, crypto exchanges are incentivized to pump up volumes to vie for better ranking and more clients. In addition, decreased volatility reduces the potential costs of wash trading (wash trading risks of capital loss in a volatile market). Therefore, lower volatility can lead to higher wash trading activities.

### 5.4. Suggestive Effects of Regulation and Implications for Policy and Industry Practice

Considering the substantial evidence and prevalent scale of wash trading in the crypto market, it is crucial to address its regulatory implications. Despite the decentralized ideal of crypto ecosystems, they remain heavily influenced by centralized exchanges that are not only vulnerable to cyberattacks, but also prone to manipulative behavior. This casts doubt on the industry's progress and supports the skepticism raised by critics about the technology's limitations and the industry's fraudulent aspects (Roubini 2018). Our findings add new insights concerning the role of regulation by demonstrating the vastly divergent trading patterns between regulated and unregulated exchanges. Without claiming causality, we offer three potential interpretations of the results.

First, regulated exchanges are required to follow the regulation, and violations are severely punished (Section 23 CRR-NY 200.3 and 200.6 of the New York Codes, Rules and Regulations; BitLicense 2015). The centralized nature of these exchanges does make direct inspections and the enforcement of regulation on crypto exchanges more feasible than on other (often anonymous) agents. For example, faking trading records are nearly impossible because regulated exchanges are required to regularly submit data "for each transaction, the amount, date, and precise time of the transaction, any payment instructions, the total amount of fees and charges received and paid to, by, or on behalf of the licensee" (23 CRR-NY 200.12, New York Codes, Rules and Regulations BitLicense 2015).[24]

Second, it is possible that compliance with regulation is costly but does not affect wash trading incentives directly. Some firms simply get a license to signal their quality (e.g., Spence 1978). This is inconsistent with the observation that, after acquiring the license, regulated exchanges still do not wash trade. Third, some unobserved exchange characteristics may cause the exchange to refrain from wash trading and acquire licenses

**Table 9.** Influence of Returns and Volatility on Wash Trading Volumes

| (log) wash trade volume$_t$ | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
|---|---|---|---|---|---|---|---|
| Weekly CMC return$_{t-1}$ | 1.258*** | | 1.444*** | | | | 1.415*** |
| | (7.14) | | (7.68) | | | | (7.16) |
| Weekly CMC return$_{t-2}$ | | 0.318** | 0.627*** | | | | 0.350** |
| | | (2.09) | (3.95) | | | | (2.22) |
| CMC volatility$_{t-1}$ | | | | −5.717*** | | −5.636*** | −4.116*** |
| | | | | (−6.06) | | (−6.03) | (−4.35) |
| CMC volatility$_{t-2}$ | | | | | −2.297** | −2.070** | −3.547*** |
| | | | | | (−2.18) | (−2.00) | (−3.15) |
| (log) wash trade volume$_{t-1}$ | 0.887*** | 0.882*** | 0.886*** | 0.885*** | 0.882*** | 0.884*** | 0.885*** |
| | (48.67) | (47.61) | (47.93) | (50.07) | (47.86) | (49.38) | (48.56) |
| Constant | 2.304*** | 2.386*** | 2.352*** | 2.543*** | 2.459*** | 2.632*** | 2.619*** |
| | (6.62) | (6.71) | (6.64) | (7.21) | (6.80) | (7.19) | (7.10) |
| Observations | 1,305 | 1,305 | 1,305 | 1,305 | 1,305 | 1,305 | 1,305 |
| Overall $R^2$, % | 92.9 | 92.7 | 93.0 | 92.9 | 92.8 | 93.0 | 93.2 |

*Notes.* This table presents the panel regression results for the impact of weekly cryptocurrency returns and volatility on wash trading volumes of unregulated exchanges. The weekly returns and volatility are calculated based on the third-party composite price indexes from CoinMarketCap (CMC). CMC volatility$_{t-1}$ is the standard deviation of daily returns during week $t-1$. Random effect models with robust errors are used in all regressions. Standard errors are clustered at exchange-currency level. $t$-statistics are reported in the brackets.

***, **, and * denote the statistical significance levels at 1%, 5%, and 10%, respectively.

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simultaneously. Such a screening function is plausible and implies that, by observing which exchanges are regulated, traders can tell whether wash trading takes place on a particular exchange.

Contrary to popular belief, the five regulated spot exchanges under BitLicense only constitute less than 3% of the total transaction volume in the cryptocurrency market based on CoinMarketCap data (October 2022). This implies that wash trading on unregulated exchanges is a first order issue that demands more regulatory attention. To address this, we provide an initial set of tools to effectively uncover wash trading and combat noncompliant and unethical behaviors. It is essential for regulatory tools and policies to be adaptive as our statistical tests may become outdated when sophisticated wash traders incorporate them into their strategies. Nevertheless, the benefits of transparency, proper regulation, and close public monitoring that we touch upon are enduring.

## 6. Conclusion

The nascency of the cryptocurrency industry provides a unique setting in which we observe both regulated and unregulated exchanges that are influential. We demonstrate that most major unregulated crypto exchanges feature excessive wash trading and warn that centralized (and vertically integrated) exchanges absent proper regulation can be problematic as seen in the collapse of FTX Trading. Specifically, we find that first digit distributions of trade size follow Benford's law for regulated exchanges, whereas nearly 30% of unregulated exchanges show violations. Regulated exchanges show apparent trade clustering at round sizes and a high level of transaction roundness, whereas for unregulated exchanges, the levels of roundness are generally low and the trade size clustering phenomenon is less prominent. Furthermore, regulated exchanges display power law distributions with exponents in the Pareto–Lévy range, consistent with other financial markets; in contrast, 20% of tier 1 and 75% of tier 2 unregulated exchanges fail to follow in any cryptocurrency.

We estimate the average wash trading to be 53.4% of trading on unregulated tier 1 exchanges and 81.8% on tier 2 exchanges and provide several robustness and validation tests. We further provide suggestive evidence that wash trading inflates exchange rankings and cryptocurrency prices and is being predicted by market signals, such as past cryptocurrency prices, and volatility and exchange characteristics, such as exchange age and user base. As likely the first comprehensive study of the pervasive crypto wash trading, our paper not only provides a cautionary tale to policymakers around the globe concerning centralized crypto exchanges, but also reminds the readers of the disciplining or screening effects of regulation in emerging industries, the importance of using wash trading–adjusted volume in certain empirical studies, and the utility of statistical tools and behavioral benchmarks for forensic finance and fraud detection. Going forward, our approaches can be further adapted to constructing wash trading metrics using publicly available data but at a lower frequency or to detect wash trading in the new nonfungible token markets.

Our study provides compelling evidence that centralized exchanges, because of their opacity, vertical integration, and lack of regulation, create ample opportunities for market manipulation, particularly by exchanges themselves. In response, consumers might be inclined to seek alternative trading venues, such as decentralized exchanges (DEXs). However, DEXs come with their own set of unique liquidity, legal, and security risks (e.g., Capponi et al. 2022). Additionally, many decentralized finance (DeFi) platforms possess suboptimal designs in fee mechanisms (Cong et al. 2022c) or interest functions (Rivera et al. 2023) that need to be improved. Future research should empirically compare market manipulation and other limitations in both CeFi institutions such as centralized exchanges and DeFi platforms. Moreover, whether centralized or decentralized, financial services should not be outside the law. Appropriate and clear regulations, as our study suggests, prove crucial for the long-term development of the industry.

### Acknowledgments

The authors are especially grateful to Agostino Capponi, Deeksha Gupta, Kose John, Tao Li, Evgeny Lyandres, and Fahad Saleh for repeated discussions and detailed feedback. The authors also thank Marlene Amstad, Mykola Babiak, Kevin Dowd, Valeria Ferrar, Itay Goldstein, Hanna Halaburda, Angel Hernando-Veciana, Andrew Karolyi, Dongyongp Lee, Minhyuk Lee, Jiasun Li, Laura Xiaolei Liu, Roger Loh, Emmanouil Platanakis, Amin Shams, Donghwa Shin, Rajeev Singhal, Baolian Wang, Shang-jin Wei, Wei Xiong, and Scott Yonker as well as seminar and conference participants and reviewers at the Alibaba Group Luohan Academy Webinar, 17th Asia-Pacific Association of Derivatives Annual Conference, Australasian Banking and Finance Conference, Behavioral Finance/Corporate Finance/Digital Finance Seminar Group, Cornell University, China International Conference in Finance 2021, Cowles Foundation for Research in Economics Conference on the Economics of Cryptocurrencies, First Crypto and Blockchain Economics Research Conference, 11th Center for the Study of Banking & Finance Conference (National Taiwan University), Durham University Department of Economics and Finance, 2021 Eastern Finance Association Annual Meeting, Econometric Society World Congress (Bocconi University), Economic Club of Memphis, European Financial Management Association Annual Meeting 2021, European Securities and Markets Authority, Federal Reserve System-Wide Webinar, 2021 Financial Management Association Annual Meeting, 11th Financial Markets and Corporate Governance Conference, 2021 Global AI Finance Research Conference, Indian Institute of Finance International Research Conference & Award Summit, Third International

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Conference on Blockchain Economics (Tokenomics 2021), 13th International Risk Management Conference, Inaugural Korea Advanced Institute of Science and Technology Digital Finance Conference, Inaugural Machine Lawyering Conference: "Human Sovereignty and Machine Efficiency in the Law," 18th Paris December Finance Meeting, Paris FinTech and Crypto Webinar, Ripple Labs London Onsite (Markets Team), 2023 Santa Clara University Crypto Conference, 60th Southwestern Finance Association Meeting, Sun Yat-sen University, Third Toronto FinTech Conference, Tsinghua University People's Bank of China School of Finance, University of California Santa Barbara-Department of Economics Defi Seminar Series, University of Central Florida, University of Technology Sydney, University of New South Wales (Sydney), University of Zurich Blockchain Center, Third University of Western Australia Blockchain and Cryptocurrency Conference, The United States Attorney's Office for the Northern District of California, Department of Justice Fraud Section/National Cryptocurrency Enforcement Team Cryptocurrency Fraud Seminar, First Virtual Symposium on Web3 Financing and Inclusivity, Inaugural Wolfram ChainScience Conference (Boston), World Finance Conference 2021, Xi'an Jiaotong University, and the Zhongnan University of Economics and Law for helpful comments. The authors have no affiliation with or research support from any cryptocurrency exchange. The contents of this publication are solely the responsibility of the authors.

## Endnotes

[1] Wash trading is defined by the U.S. Commodity Exchange Act as "entering into, or purporting to enter into, transactions to give the appearance that purchases and sales have been made, without incurring market risk or changing the trader's market position." In other words, wash trading occurs when someone fabricates trades and acts as the counterparty on both sides to inflate volume. The definition of wash trading from the U.S. Commodity Exchange Act can be found at: https://www.cftc.gov/LearnAndProtect/AdvisoriesAndArticles/CFTCGlossary/index.htm#W.

[2] Our research was consulted to assist federal investigations and legislation by the U.S. Department of Justice, the Securities Exchange Commission, New York State Office of Attorney General, and the Federal Bureau of Investigation.

[3] Individuals can wash trade as well. It is documented that traders use cryptocurrency and nonfungible token wash trading to net millions of profits (Quiroz-Gutierrez 2022, Cong, Landsman, Maydew, and Rabetti 2023b).

[4] For example, Bitwise Asset Management suggested to the SEC in 2019 potential wash trading on crypto exchanges (Fusaro and Hougan 2019), but the allegations were denied by the exchanges (see https://cryptonews.net/news/market/235179/ and https://blokt.com/news/alameda-research-bitwise-report-on-fake-bitcoin-trading-volume-inaccurate).

[5] Cong et al. (2020, 2022a), Lyandres et al. (2022), Howell et al. (2020), and Cong and Xiao (2021) provide further institutional background on cryptocurrencies and initial coin offerings (ICOs); a number of articles discuss the role of crypto-tokens in fundraising and commitment (e.g., Goldstein et al. 2019); and studies such as Liu and Tsyvinski (2021) and Shams (2020) document empirical patterns in cryptocurrency returns. With respect to nonfinancial aspects of cryptocurrencies, see Halaburda et al. (2022) for a discussion of cryptocurrencies' design and references therein.

[6] Our paper, therefore, contributes to forensic finance—the application of economic and financial knowledge to discover or substantiate evidence of criminal wrongdoing that meets standards in a court of law (e.g., Allen and Gale 1992, Jarrow 1992, Christie and Schultz 1994, Ritter 2008, Zitzewitz 2012). Recently, blockchain forensics have been applied to on-chain data to study cybercrimes (e.g., Cong et al. 2022b, 2023a).

[7] There may be concerns that our data could disproportionately represent exchanges with a higher prevalence of wash trading. However, the data set spans a wide range of ranks (1–300 among crypto exchanges), and as we later illustrate, even lower ranked exchanges are highly incentivized to engage in wash trading. Moreover, TokenInsight evaluates representativeness beyond mere rankings when choosing exchanges to analyze. Some exchanges that became prominent in subsequent years, such as FTX, had not yet been established and are not covered in our data.

[8] Because U.S. dollars are only allowed to exchange in three U.S.-regulated exchanges (Bitstamp, Coinbase, and Gemini), digital dollars (symbol USDT, also known as stablecoins, which are designed to be pegged to the U.S. dollar) are commonly used as substitutes and widely accepted by most trading platforms. We treat cryptocurrency–USD pairs and cryptocurrency–USDT pairs as being the same in this study.

[9] BitLicense requires an exchange to build a sophisticated compliance system, an anti–money laundering program, a capital control and custodian system, a record-keeping and customer identity system, an information security team, and a disaster recovery system as well as to submit necessary documents for routine checks, which cost between 20,000 to 100,000 U.S. dollars even for compliant exchanges (Perez 2015).

[10] Tier 2 unregulated exchanges in our sample all ranked lower than 960. This distinction of tiers does not affect any of our results because they are mostly at the exchange level.

[11] The Singaporean authority integrated crypto exchanges into the existing systems by requiring crypto exchanges to comply with the new Payment Services Act (https://www.mas.gov.sg/regulation/guidelines/ps-g02-guidelines-on-provision-of-digital-payment-token-services-to-the-public). The Swiss Financial Market Supervisory Authority issued several guidelines and ordinances to regulate distributed ledger technology trading facilities and ICOs (www.finma.ch/en/authorisation/fintech/). The Japanese Financial Services Agency and the British Financial Conduct Authority have also established their own crypto regulations.

[12] LTC/USD data are not available on Liquid, Bgogo, Lbank, and Exmo. XRP/USD data are not available on Gemini, Bgogo, and Lbank.

[13] Benford's law is most widely known and applied to examine the first significant digit distribution of a data set. The law also makes predictions about the distribution of second digits, third digits, digit combinations, and so on. Here, in this research, only the first significant digit part of Benford's law is applied to avoid interference from other behavioral biases.

[14] See https://info.exmo.com/en/platform-features/what-is-exmocoin/ and https://www.coindesk.com/markets/2018/06/22/fcoin-crypto-exchange-draws-fire-for-controversial-business-model/.

[15] We focus on clustering in terms of round numbers in the number of tokens instead of dollar amounts because our data contains the number of tokens traded, and its product with token price is typically not equal to the actual dollar amount traders use in their orders because of exchange fees. For a few exchanges for which we can obtain the time series of fees, we verify our results to be robust to the alternative specification using dollar amounts.

[16] Rounding could lead to violations of Benford's law for later digits, yet the first significant digits still follow Benford's law as seen in multiple forensic applications (e.g., Carslaw 1988, Thomas 1989).

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[17] For example, power law distribution of tails can be found in Pareto distribution of income (Pareto 1896), the distribution of stock returns (Gopikrishnan et al. 1999), trade size (Gopikrishnan et al. 2000), share volume (Plerou et al. 2000), fluctuations in foreign exchange markets (Vandewalle et al. 1997, Da Silva et al. 2007, Ohnishi et al. 2008), and cryptocurrency transactions (Li et al. 2019, Schnaubelt et al. 2019).

[18] Gopikrishnan et al. (2000) find that the power law exponent of trade volume is around 1.5 in the U.S. equity market. Plerou and Stanley (2007) investigate trades in the New York Stock Exchange, London Stock Exchange, and Paris Bourse and show that trade size in all three markets display the power law decay with exponents in the range from one to two. Moreover, the value of exponents is not affected by industry and market capitalization. Note that Mandelbrot (1960) propose that income follows the stable Pareto–Lévy distributions with $1 < \alpha < 2$.

[19] For 1.01 BTC, the place value of the last nonzero digit (1) is hundredths, whereas the place value of the last nonzero digit (3) is thousandths in 2.123 BTC. In 100 ETH, the place value of the last nonzero digit (1) is hundreds, whereas the place value of the last nonzero digit (4) is ones in 1,234 ETH.

[20] For instance, according to SimilarWeb reports, CoinMarketCap contributes 65% of web traffic to one regulated exchange in our sample. It serves as the leading referral website and contributes most of the traffic to 20 unregulated exchanges. Furthermore, 17 of these unregulated exchanges receive more than 30% of their total web traffic from CoinMarketCap referrals.

[21] Because crypto exchanges are not listed, we do not observe exchanges' revenues and profits. But we can estimate exchanges' profit for the ones that issue their own tokens with utility and dividend functions. Such exchanges periodically use a portion of their operating profit to buy back and destroy tokens from the secondary market (monthly or quarterly). We manually collect all available buyback reports and token white papers from exchanges' website to compute the value of the tokens bought back or burned. Then, with the buyback/profit ratio the exchanges promise (typically described) in the exchange tokens' white papers, we calculate the exchanges' profits. In our sample, Binance, Bitfinex, Huobi, KuCoin, Okex, Zb, Bgogo, BitZ, Mxc, Bibox, and Bitmart issue exchange tokens and have data available. We find an exchange's profit is positively correlated with both the reported volume and our estimated real volume. In an unreported pooled regression controlling for week fixed effect, the coefficient of log profit on log real volume is 0.85 and significant at a 1% level. We also find that reported CoinMarketCap volume positively and significantly predicts the subsequent week's nonwash trading volume, consistent with the intuition and empirical findings in Amiram et al. (2021).

[22] We extract 2016–2018 GDP and financial access data from the World Bank Databank. The measurement of finance access includes the number of commercial bank branches (per 100,000 adults), account ownership at a financial institution, and the number of ATMs (per 100,000 adults). The average value of GDP and financial access measurement is used to rank all traffic countries in our sample.

[23] Note that the weekly volatility is calculated using daily returns in the week. All regressions employ random effects with robust errors.

[24] Regulators with basic forensic tools can easily find wash-trading evidence with this level of trading records. For example, the exchange account carrying wash-trading activities are likely to exhibit abnormally large volume as well as unusual behavior patterns (such as Willy and Markus in Mt. Gox). Besides, wash-trading volume does not bring trading fee revenues, so exchanges need to work hard to cover the tells in the balance sheet. Regulators can also find suspicious wash trading from the trading volume and user scale and custodian asset size.

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