# Lynn Heller

Curriculum Vitae

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#### Personal Details

Date of Birth October 31st, 1985 in Wuhan.

Nationality German.

Marital status Married, 3 children.

## Research Interests

I aim at answering differential geometric questions arising in the study of minimal and constant mean curvature surfaces as well as (constrained) Willmore surfaces (in 3—dimensional space forms) by combining techniques from geometric analysis, integrable systems (e.g., Hitchin system) and algebraic geometry (e.g., Higgs bundles and moduli spaces). Recently, we discovered a surprising connection to number theory, when alternating multiple zeta values naturally appeared in our computations.

## Employment

Since 09/2022 **Professor** at Yanqi Lake Beijing Institute of Mathematical Sciences and Applications.

04/2017–08/2022 Juniorprofessor in Pure Mathematics at Leibniz Universität Hannover.

04/2014-03/2017 Margarete von Wrangell fellow at Eberhard Karls University Tübingen.

01/2013-03/2014 **PostDoc** at Eberhard Karls University Tübingen.

01/2009-06/2012 PhD student at Eberhard Karls University Tübingen.

#### Education

2020 **Positive interims evaluation of the Juniorprofessorship**, equivalent to the German Habilitation, Leibniz Universität Hannover.

2009–2012 PhD in Mathematics, Eberhard Karls University Tübingen.

Thesis title: Equivariant Constrained Willmore Tori in  $S^3$ .

Advisor: Prof. Dr. Franz Pedit.

2003–2008 Diplom (MSc equivalent) in Mathematics, TU Berlin.

Diplom thesis advisor: Prof. Dr. Ulrich Pinkall.

2003–2007 Diplom (MSc equivalent) in Business Administration, FU Berlin.

### Awards and Grants

- 05/2023 Organizer of the BIRS-IMAG workshop "Minimal surfaces in symmetric spaces" joint with Francesco Martin (Granada), Rafael Montezuma (Fortaleza), Franz Pedit (UMass, Amherst), and Mike Wolf (Georgia Tech)
- 07/2021 Organizer and speaker at the MSRI Summer Graduate School "Gauge Theory in Geometry and Topology" joint with Francesco Lin (Columbia), Laura Starkston (UC Davis) und Boyu Zhang (Princeton)
- Since 2017 **Member and project leader** within the DFG priority programm "Geometry at Infinity" with the project *Minimizers of the Willmore energy with prescribed rectangular conformal class* (11.000 Euro) and with the project *Large Genus Limit of Energy Minimizing Compact Minimal Surfaces in the 3-Sphere* (~ 150.000 Euro)
- 2015-2017 **Research grant** within the "Eliteprogramm für PostdoktorandInnen" (PI) of the state Baden-Württemberg. (125.000 Euro)
- 2014–2017 Margarete von Wrangell fellowship of the state Baden-Würtemberg and the European Social Fund. (~ 200.000 Euro)
  - 2014 Participant of the second Heidelberg Laureates Forum.
- 2013–2014 **Research grant** "Projektförderung für NachwuchswissenschaftlerInnen" (PI) within the excellence Initiative of the Eberhard Karls University Tübingen. ( $\sim 35.000 \text{ Euro}$ )

#### Publications

#### Accepted and published

The five most important publications are highlighted in green.

- 1. L. Heller, S. Heller. Fuchsian DPW potentials for Lawson surfaces. Geom Dedicata, volume 217, paper no. 101, 21 pages, 2023.
- 2. L. Heller, S. Heller, M. Traizet. Area estimates for high genus Lawson surfaces via DPW. J. Differ. Geom., volume 124, no. 1, pp 1–35, 2023
- 3. L. Heller, C. B. Ndiaye. First explicit constrained Willmore minimizers of non-rectangular conformal class. Adv. Math. volume 386, paper no. 107804, 47 pages, 2021.
- 4. L. Heller, Ch. B. Ndiaye. Candidates for non-rectangular constrained Willmore minimizers. J. Geom. Phys. volume 165, paper no. 104221, 35 pages, 2021.
- 5. L. Heller, S. Heller, Ch. B. Ndiaye. Stability properties of 2-lobed Delaunay tori in the 3-sphere. Differ. Geom. Appl. volume 79, paper no. 101805, 2021.
- 6. L. Heller, S. Heller, Ch. B. Ndiaye. *Isothermic constrained Willmore tori in 3-space*. **Ann. Glob. Anal. Geom.** volume 60, pp 231–251, 2021.
- 7. L. Heller, Generalized Whitham Flow and its Applications. Minimal surfaces: Integrable Systems and Visualisation, Springer Proceedings in Mathematics & Statistics 349, pp 131–146, 2021.
- 8. L. Heller, S. Heller, Higher solutions of Hitchin's self-duality equations. **J. Int. Syst.** volume 5, no. 1, xyaa006, 42 pages, 2020.
- 9. L. Heller, F. Pedit, *Towards a constrained Willmore conjecture*. Willmore energy and Willmore conjecture, pp 119–138, Monogr. Res. Notes Math., CRC Press, Boca Raton, FL, 2018.

- 10. L. Heller, S. Heller, N. Schmitt Navigating the Space of Symmetric CMC Surfaces. J. Differ. Geom. volume 110, no. 3, pp 413–455, 2018.
- 11. L. Heller. *Dirac Tori*. **Differ. Geom. Appl.** volume 54, Part A, pp 122–128, 2017.
- 12. L. Heller, S. Heller. Abelianization of Fuchsian systems on a 4-punctured sphere and applications. J. Symplect. Geom. volume 14, no. 4, pp 1059–1088, 2016.
- 13. L. Heller, S. Heller, N. Schmitt. Spectral curve theory for (k, l)-Symmetric CMC Surfaces of Higher Genus. J. Geom. Phys. volume 98, pp 201–213, 2015.
- 14. L. Heller. Constrained Willmore and CMC Tori in the 3-Sphere. **Differ. Geom.** Appl. volume 40, pp 232–242, 2015.
- 15. L. Heller. Equivariant Constrained Willmore Tori in the 3-Sphere. Math. Z. volume 278, no. 3, pp 955-977, 2014.
- 16. L. Heller, Constrained Willmore Tori and Elastic Curves in 2-Dimensional Space Forms. Comm. Anal. Geom. volume 22, no. 2, pp 343–369, 2014.
- 17. L. Heller. Constrained Willmore Hopf tori. Oberwolfach Reports, voume 10, no. 2, 2013.
- 18. L. Heller. *Equivariant Constrained Willmore Tori in S*<sup>3</sup>. PhD Thesis, Eberhard Karls University Tübingen, 2012.

#### **Preprints**

- 19. L. Heller, S. Heller, N. Schmitt, Exploring the Space of Compact Symmetric CMC Surfaces. Preprint: arXiv: 1503.07838.
- 20. I. Biswas, S. Dumitrescu, L. Heller, S. Heller. Holomorphic systems with Fuchsian monodromy (with an appendix by Takuro Mochizuki). **38 pages**, preprint: arXiv:2104.04818.
- 21. L. Heller, S. Heller, M. Traizet. Complete families of embedded high genus CMC surfaces in the 3-sphere (with an appendix by Steven Charlton). 42 pages, preprint: arXiv:2108.10214.
- 22. I. Biswas, S. Dumitrescu, L. Heller, S. Heller, On the existence of holomorphic curves in compact quotients of SL(2,C). 33 pages, preprint: arXiv:2112.03131.
- 23. L. Heller, S. Heller, M. Traizet. Loop group methods for the non-abelian Hodge correspondence on a 4-punctured sphere. **45 pages**, preprint: arXiv:2205.12106.
- 24. I. Biswas, L. Heller, S. Heller. *Holomorphic Higgs bundles over the Teichmüller space*. **14 pages**, preprint: arXiv:2308.13860.

#### Selected Invited Talks

- 08/2023 "Lawson surfaces and multiple zeta values", Matrix Workshop on "Spectrum and Symmetry for Group Actions in Differential Geometry II", Creswick, Australia.
- 07/2023 "Lawon surfaces and multiple zeta values", International Congress of Basic Science, Beijing, China.
- 03/2022 Lecture series at the 13th MSJ-SI 2021 "Differential Geometry and Integrable Systems". 3 lectures at the school and 1 lecture at the international conference at the 3 weeks event about "Complete families of high genus CMC surfaces in the 3-sphere".

- 07/2021 Lecture series at the (online) MSRI Summer Graduate School "Gauge theory in Geometry and Topology". 5 lectures about "Harmonic maps into 3-dimensional space forms".
- 06/2020 Area estimates of high genus Lawson surfaces via DPW. Online-Seminar "Geometric Analysis".
- 05/2020 Higher solutions to Hitchin's self-duality equations and Willmore surfaces. Online-lecture the joint seminar: Bochum Essen Köln Wuppertal: "Complex Algebraic Geometry and Complex Analysis".
- 01/2020 Area estimates of high genus Lawson surfaces via DPW. "Topics in Geometric Analysis", FU Berlin.
- 12/2019 Isothermic constrained Willmore tori in the 3-sphere. Three talks at the workshop "Geometry of Submanifolds and Integrable Systems", Osaka, Japan.
- 03/2019 Higher solutions to Hitchin's self-duality equations and Willmore surfaces. Workshop on Challenges at the Interface of Hitchin Systems and String Theory, Simons Center for Geometry and Physics, Stony Brook, USA
- 07/2018 Higher solutions to Hitchin's self-duality equations. BIRS-CMO Workshop, "Higgs Bundles and Harmonic Maps of Riemann Surfaces", Oaxaca, Mexico.
- 03/2018 Recent progress in integrable surface theory. Workshop: Geometry of Submanifolds and Integrable Systems, Osaka City University, Japan.
- 01/2018 Willmore surfaces and higher solutions of Hitchin's self-duality equations. Minimal Surfaces and related topics, University of Granada, Spain.
- 05/2017 Constrained Willmore Minimizers. LMS Workshop on Variational Methods in Submanifold Theory, York, England.
- 04/2017 Constrained Willmore Minimizers. Analysis seminar, UMass, Amherst, USA.
- 06/2016 Constrained Willmore Minimizer. 38th Southern-German Differential Geometry Colloquium, Mainz.
- 04/2016 An integrable systems approach to surface theory. Loughborough University.
- 02/2016 Deformation theory of spectral data. OCAMI-KOBE-WASEDA Joint International Workshop on Differential Geometry and Integrable Systems, Osaka City University, Japan.
- 12/2015  $\,$  Abelianization of Fuchsian Systems and Applications. Tsinghua University, Beijing, China.
- 11/2015 Higher genus constant mean curvature surfaces in the 3-sphere. Yorkshire Durham Geometry Days, University of York.
- 08/2015 Navigating the space of symmetric CMC surfaces. George Boole Mathematical Sciences Conference, Theme 4: Geometry and Visualization, University College Cork.
- 05/2015 Moduli spaces, integrable systems and applications to surface theory. Meeting of the German chapter of European Women in Mathematics, Rauischholzhausen.
- 12/2014 Abelianization of Fuchsian Systems and its Application to Surface Theory. Oberseminar Differentialgeometrie, WWU Münster.
- 06/2014 Constrained Willmore Minimizers Theory and Experiments. KiS Seminar, TU Berlin
- 11/2013 Constrained Willmore Hopf tori. Pure mathematics seminar, University of Leicester.

- 05/2013 Constrained Willmore Tori and Elastic Curves. Workshop on Progress in Surface Theory, MFO Oberwolfach.
- 03/2012 Equivariant Constrained Willmore Tori in the 3-Sphere. Hausdorff Trimester Programm: Integrability in Geometry and Mathematical Physics, HIM Bonn.

## Teaching experience

#### Courses as instructor of record

- SS 21 Geometrie für Sonderpädagogen (elementary geometry for teachers), Reading Seminar Differential Geometrie (topic: h-principle)
- WS 20/21 Riemannsche Geomtrie (Riemannian Geometry)
  - SS 20 Mathematik für Physiker 2 (Complex Analysis and Laplace equations), Complex Analysis, Geometrie für Sonderpädagogen (elementary Geometry for teachers)
- WS 19/20 Mathematik für Physiker I (integration theory)
  - SS 19 Riemann surfaces and complex differential geometry
- WS 18/19 Riemannsche Geomtrie (Riemannian geometry)
  - SS 18 Analysis B (multivariate calculus for computer science students), Harmonische Abbildungen (harmonic maps)
- WS 17/18 Riemannsche Flächen (Riemann surfaces)
  - SS 17 Klassische Differentialgeometrie (classical differential geometry)
  - SS 16 Gewöhnliche Differentialgleichungen (ordinary differential equations)
- WS 15/16 Quaternionische Flächentheorie (quaternionic surface theory)
  - SS 15 Klassifikation kompakter Flächen (classification of compact surfaces)
- WS 14/15 Proseminar: Kurven (curves)
- WS 13/14 Proseminar: Projektive Geometrie

#### PhD Students

since 09/2023 Bochuan Liu

since 10/2021 Balázs Márk Békési

since 04/2018 Daniel Holzwart

04/2017-05/2021 Max Heydel

#### PostDocs

9/2020-082022 Thomas Raujouan

03/2016-08/2017 Nicholas Schmitt

01/2016-06/2016 Cheikh Birahim Ndiaye

#### Miscellanea

- Since 11/2022 Managing editor of the ICCM Notices
- 01/2020–07/2022 Equal opportunity officer of the faculty for Mathematics and Physics, Leibniz Universität Hannover
  - 08/2017 Organization of the Workshop "Higgs bundles, harmonic maps and integrable systems", Leibniz Universität Hannover
  - 2011-2017 Equal opportunity officer of the mathematics institute in Tübingen.
    - 2014 Participation in the NIMS-IMAGINARY exhibition at the ICM in Seoul.

- 2013/2014~ Organization of mathematics workshops for children within the "Kinder-Uni-Forschertag" in Tübingen.
  - 2013 Participation in the exhibition "Wie Schönes Wissen Schafft" at the Museum of the University of Tübingen.

September 16, 2023