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Education and Research Experience

2024 – *current* Beijing Institute of Mathematical Sciences and Applications
Assistant Professor, tenure track

2022 – 2024 Institute for Information Transmission Problems, Russia
Senior Researcher

2021 – 2022 University of Geneva, Switzerland
Department of Mathematics
Senior Researcher

2019 – 2020 Uppsala University, Sweden
Department of Mathematics
Researcher

2015 – 2018 Harvard University, Cambridge, USA
Harvard Society of Fellows and Department of Mathematics
Junior Fellow

2011 – 2015 University of California, Berkeley, USA
Department of Mathematics
Graduate student
Advisors: Mina Aganagic, Nikolai Reshetkin
Ph.D. in Mathematics, June 2015

2009 – 2010 Institute for Theoretical and Experimental Physics (ITEP), Moscow, Russia
Junior Researcher

2007 – 2009 Moscow Institute of Physics and Technology (MIPT), Moscow, Russia
M.S. in Physics, June 2009

2005 – 2007 Moscow Institute of Physics and Technology (MIPT), Moscow, Russia
B.S. in Physics, June 2007

2002 – 2005 Kazan State University (KSU), Kazan, Russia

Honors and Awards

2017 – 2018	Milton Fund Award, Harvard University, USA
2015 – 2018	Harvard Junior Fellowship, Harvard University, USA
2015	Simons Junior Fellowship, Simons Foundation, USA (offer)
2008 – 2009	Moebius Foundation Fellowship, Russia
2008	1st place award at the Russian Moebius contest for the best research paper in mathematics and mathematical physics Paper: <i>Analogue of the identity $\text{Log Det} = \text{Trace Log for resultants}$</i> [44]
2008	Weisskopf diploma, 46rd International School of Subnuclear Physics, Italy
2007 - 2008	Dynasty Foundation Fellowship, Russia

Research Interests

I am a mathematician working in the field of Representation Theory with focus on relation to geometry, particularly Topology (quantum group invariants of knots, links and 3-manifolds, mapping class groups of surfaces, q-skein and double affine Hecke algebras) and Algebraic Geometry (representations of quantum Virasoro and \mathcal{W} -algebras associated with cohomology and K-theory of Nakajima quiver varieties). The role and importance of Mathematical Physics (topological quantum field theory, integrable systems, instantons and the String-Math interaction) in these domains has been increasingly recognized; my research is substantially inspired by advances in mathematical physics and benefits from recurring collaboration with physicists. This picture is complemented by my work on the interface with Probability (integrable probabilistic systems, Macdonald processes and random matrices) and a long-standing interest in Classical Invariant Theory (invariants of curves and surfaces, tensors, discriminants and resultants of algebraic equations). Key recent results that illustrate my research program include construction of a genus two analogue of the double affine Hecke algebra [14], formulation of a double elliptic generalization of Macdonald difference equations [8], development of a new method to compute observables of Macdonald processes [22], proof of a determinantal formula for the Cayley invariant of plane curves [24] among others.

Publication List

- 1 H.Awata, K.Hasegawa, H.Kanno, R.Ohkawa, Sh.Shakirov, J.Shiraishi, Y.Yamada
*Non-stationary difference equation and affine Laumon space II:
Quantum Knizhnik-Zamolodchikov equation*
SIGMA 20 (2024), 077
<https://arxiv.org/abs/2309.15364>
- 2 S. Arthamonov, Sh. Shakirov
An Elliptic Generalization of A1 Spherical DAHA at K=2
International Mathematics Research Notices 19 (2024) 13046–13084
<https://doi.org/10.1093/imrn/rnae192>
<https://arxiv.org/abs/2306.00215>
- 3 H.Awata, K.Hasegawa, H.Kanno, R.Ohkawa, Sh.Shakirov, J.Shiraishi, Y.Yamada
*Non-stationary difference equation and affine Laumon space:
Quantization of discrete Painlev'e equation*
SIGMA 19 (2023), 089
<https://arxiv.org/abs/2211.16772>
- 4 Sh. Shakirov
Non-stationary difference equation for q-Virasoro conformal blocks
Letters in Mathematical Physics 114 (2024) 115
<https://doi.org/10.1007/s11005-024-01856-2>
<https://arxiv.org/abs/2111.07939>
- 5 A. Gorsky, P. Koroteev, O. Koroteeva, Sh. Shakirov
Double Inozemtsev Limits of the Quantum DELL System
Phys.Lett.B 826 (2022) 136919
<https://doi.org/10.48550/arXiv.2110.02157>
<https://arxiv.org/abs/2110.02157>
- 6 A.Morozov, A.Popolitov and Sh. Shakirov
Harer-Zagier formulas for knot matrix models
Phys.Lett.B 818 (2021) 136370
<https://doi.org/10.1016/j.physletb.2021.136370>
<https://arxiv.org/abs/2102.11187>
- 7 A.Morozov, A.Popolitov and Sh. Shakirov
Quantization of Harer-Zagier formulas
Phys.Lett.B 811 (2020) 135932
<https://doi.org/10.1016/j.physletb.2020.135932>
<https://arxiv.org/abs/2008.09577>

- 8 P.Koroteev and Sh.Shakirov
The Quantum DELL System
Lett. Math. Phys. 110 (2020) 969–999
<https://doi.org/10.1007/s11005-019-01247-y>
<https://arxiv.org/abs/1906.10354>

- 9 R. Lodin, A. Popolitov, Sh. Shakirov and M. Zabzine
Solving q -Virasoro constraints
Lett. Math. Phys. 110 (2020) 179–210
<https://doi.org/10.1007/s11005-019-01216-5>
<https://arxiv.org/abs/1810.00761>

- 10 C. Kozaz, Sh. Shakirov, C. Vafa and W. Yan
Refined Topological Branes
Comm. Math. Phys. 385 (2021) 937–961
<https://doi.org/10.1007/s00220-020-03883-1>
<http://arxiv.org/abs/1805.00993>

- 11 A. Morozov, A. Popolitov and Sh. Shakirov
On (q,t) -deformation of Gaussian matrix model
Phys. Lett. B 784 (2018) 342–344
<https://doi.org/10.1016/j.physletb.2018.08.006>
<http://arxiv.org/abs/1803.11401>

- 12 C. Kozcaz, Sh. Shakirov and W. Yan
Argyres-Douglas Theories, Modularity of Minimal Models and Refined Chern-Simons
Adv.Theor.Math.Phys. 26 (2022) 3, 643–672
<https://dx.doi.org/10.4310/ATMP.2022.v26.n3.a3>
<http://arxiv.org/abs/1801.08316>

- 13 L. Bishler, An. Morozov, A. Sleptsov and Sh. Shakirov
On the block structure of the quantum R-matrix in the three-strand braids
Int. J. Mod. Phys. A 33 N. 17 (2018) 1850105
<https://doi.org/10.1142/S0217751X18501051>
<http://arxiv.org/abs/1712.07034>

- 14 S.Arthamonov and Sh.Shakirov
Genus Two Generalization of A_1 spherical DAHA
Selecta Mathematica 25 (2019) 17
<https://doi.org/10.1007/s00029-019-0447-1>
<http://arxiv.org/abs/1704.02947>

- 15 Sh. Shakirov and A. Sleptsov
Quantum Racah matrices and 3-strand braids in representation [3,3]
J. Geom. Phys. 166 (2021) 104273
<https://doi.org/10.1016/j.geomphys.2021.104273>
<http://arxiv.org/abs/arXiv:1611.03797>

- 16 Clay Cordova, Ben Heidenreich, Alexandr Popolitov, Shamil Shakirov
Orbifolds and Exact Solutions of Strongly-Coupled Matrix Models
Comm. Math. Phys. 361 (2018) 1235–1274
<https://doi.org/10.1007/s00220-017-3072-x>
<http://arxiv.org/abs/1611.03142>

- 17 S.Arthamonov and Sh.Shakirov
Refined Chern-Simons Theory in Genus Two
J. Knot Theory Ram. 29 N. 07 (2020) 2050044
<https://doi.org/10.1142/S0218216520500443>
<http://arxiv.org/abs/1504.02620>

- 18 M.Aganagic and Sh.Shakirov
Gauge/Vortex duality and AGT
in *New Dualities of Supersymmetric Gauge Theories*,
Mathematical Physics Studies, Springer, 2016
<http://arxiv.org/abs/1412.7132>

- 19 M.Aganagic, N.Haouzi and Sh.Shakirov
A-n Triality
<http://arxiv.org/abs/1403.3657>

- 20 M.Aganagic, N.Haouzi, C.Kozcaz and Sh.Shakirov
Gauge/Liouville Triality
Comm.Math.Phys., accepted <http://arxiv.org/abs/1309.1687>

- 21 Sh. Shakirov
Colored knot amplitudes and Hall-Littlewood polynomials
<http://arxiv.org/abs/1308.3838>

- 22 A. Borodin, I. Corwin, V. Gorin and Sh. Shakirov
Observables of Macdonald processes
Trans. Amer. Math. Soc. 368 (2016) 1517-1558
<https://doi.org/10.1090/tran/6359>
<http://arxiv.org/abs/1306.0659>

- 23 M. Aganagic and Sh. Shakirov
Refined Chern-Simons Theory and Topological String
<http://arxiv.org/abs/1210.2733>

- 24 A. Popolitov and Sh. Shakirov
On Undulation Invariants of Plane Curves
Michigan Math. J. 64-1 (2015) 143-153
<https://doi.org/10.1307/mmj/1427203288>
<http://arxiv.org/abs/1208.5775>

- 25 A.Mironov, A.Morozov and Sh.Shakirov
Torus HOMFLY as the Hall-Littlewood Polynomials
J. Phys. A: Math. Theor. 45 (2012) 355202
<http://arxiv.org/abs/1203.0667>

- 26 A. Mironov, A. Morozov, Sh. Shakirov and A. Sleptsov
*Interplay between MacDonald and Hall-Littlewood expansions
of extended torus superpolynomials*
JHEP 2012 (2012) 70
<http://arxiv.org/abs/1201.3339>

- 27 M. Aganagic and Sh. Shakirov
Knot Homology from Refined Chern-Simons Theory
Comm.Math.Phys. 333 (2015) 187-228
<https://doi.org/10.1007/s00220-014-2197-4>
<http://arxiv.org/abs/1105.5117>

- 28 A.Mironov, A.Morozov, Sh.Shakirov and A.Smirnov
Proving AGT conjecture as HS duality: extension to five dimensions
Nucl. Phys. B 855 (2012) 128-151
<https://doi.org/10.1016/j.nuclphysb.2011.09.021>
<http://arxiv.org/abs/1105.0948>

- 29 A.Mironov, A.Morozov, A.Popolitov and Sh.Shakirov
Resolvents and Seiberg-Witten representation for Gaussian beta-ensemble
Theor. Math. Phys. 171:1 (2012) 505-522
<https://doi.org/10.1007/s11232-012-0049-y>
<http://arxiv.org/abs/1103.5470>

- 30 A.Mironov, A.Morozov and Sh.Shakirov
A direct proof of AGT conjecture at $\beta = 1$
JHEP 1102 (2011) 067
[https://doi.org/10.1007/JHEP02\(2011\)067](https://doi.org/10.1007/JHEP02(2011)067)
<http://arxiv.org/abs/1012.3137>

- 31 A.Mironov, A.Morozov and Sh.Shakirov
Towards a proof of AGT conjecture by methods of matrix models
Int. J. Mod. Phys. A 27 (2012) 1230001
<https://doi.org/10.1142/S0217751X12300013>
<http://arxiv.org/abs/1011.5629>

- 32 A.Mironov, A.Morozov and Sh.Shakirov
Brezin-Gross-Witten model as the pure gauge limit of Selberg correlators
JHEP 1103 (2011) 102
[https://doi.org/10.1007/JHEP03\(2011\)102](https://doi.org/10.1007/JHEP03(2011)102)
<http://arxiv.org/abs/1011.3481>

- 33 A.Mironov, A.Morozov and Sh.Shakirov
On Dotsenko-Fateev representation of the toric conformal blocks
J. Phys. A 44 (2011) 085401
<https://doi.org/10.1088/1751-8113/44/8/085401>
<http://arxiv.org/abs/1010.1734>

- 34 A.Morozov and Sh.Shakirov
From Brezin-Hikami to Harer-Zagier formulas for Gaussian correlators
<http://arxiv.org/abs/1007.4100>

- 35 A.Morozov and Sh.Shakirov
The matrix model version of AGT conjecture and CIV-DV prepotential
JHEP 1008 (2010) 066
[https://doi.org/10.1007/JHEP08\(2010\)066](https://doi.org/10.1007/JHEP08(2010)066)
<http://arxiv.org/abs/1004.2917>

- 36 A.Mironov, A.Morozov and Sh.Shakirov
Conformal blocks as Dotsenko-Fateev integral discriminants
Int. J. Mod. Phys. A 25 (2010) 3173-3207
<https://doi.org/10.1142/S0217751X10049141>
<http://arxiv.org/abs/1001.0563>

- 37 Sh.Shakirov
Exact solution for mean energy of 2d Dyson gas at $\beta = 1$
Phys. Lett. A 375 (2011) 984-989
<https://doi.org/10.1016/j.physleta.2011.01.004>
<http://arxiv.org/abs/0912.5520>
- 38 A.Mironov, A.Morozov and Sh.Shakirov
Matrix model conjecture for exact BS periods and Nekrasov Functions
JHEP 1002 (2010) 030
[https://doi.org/10.1007/JHEP02\(2010\)030](https://doi.org/10.1007/JHEP02(2010)030)
<http://arxiv.org/abs/0911.5721>
- 39 A.Morozov and Sh.Shakirov
New and Old Results in Resultant theory
Theor. Math. Phys. 163:2 (2010) 587-617
<https://doi.org/10.1007/s11232-010-0044-0>
<http://arxiv.org/abs/0911.5278>
- 40 N.Perminov and Sh.Shakirov
Discriminants of Symmetric Polynomials
<http://arxiv.org/abs/0910.5757>
- 41 A.Morozov and Sh.Shakirov
On Equivalence of two Hurwitz Matrix Models
Mod. Phys. Lett. A, Vol. 24, No. 33 (2009) 2659-2666
<https://doi.org/10.1142/S0217732309031995>
<http://arxiv.org/abs/0906.2573>
- 42 A.Morozov and Sh.Shakirov
Exact 2-point function in Hermitian matrix model
JHEP 0912 (2009) 003
<http://arxiv.org/abs/0906.0036>
- 43 A.Morozov and Sh.Shakirov
Introduction to Integral Discriminants
JHEP 0912 (2009) 002
[https://doi.org/10.1007/JHEP12\(2009\)002](https://doi.org/10.1007/JHEP12(2009)002)
<http://arxiv.org/abs/0903.2595>
- 44 A.Morozov and Sh.Shakirov
Generation of matrix models by W-operators
JHEP 0904 (2009) 064
[https://doi.org/10.1007/JHEP04\(2009\)064](https://doi.org/10.1007/JHEP04(2009)064)
<http://arxiv.org/abs/0902.2627>

- 45 A.Anokhina, A.Morozov and Sh.Shakirov
Resultant as the determinant of Koszul complex
Theoretical and Mathematical Physics 160:3 (2009) 1203-1228
<https://doi.org/10.1007/s11232-009-0111-6>
<http://arxiv.org/abs/0812.5013>
- 46 A.Morozov and Sh.Shakirov
Resultants and contour integrals
Funct. Anal. Appl. 46 (2012) 33-40
<https://doi.org/10.1007/s10688-012-0004-6>
<http://arxiv.org/abs/0807.4539>
- 47 A.Morozov and Sh.Shakirov
Analogue of the identity $\text{Log Det} = \text{Trace Log}$ for resultants
Geom. Phys. 61 (2010) 708-726
<https://doi.org/10.1016/J.GEOMPHYS.2010.12.001>
<http://arxiv.org/abs/0804.4632>
- 48 E.Akhmedov and Sh.Shakirov
Gluing of surfaces with polygonal boundaries
Funct. Anal. Appl. 43 (2009) 245-253
<https://doi.org/10.1007/s10688-009-0033-y>
<http://arxiv.org/abs/0712.2448>
- 49 V.Dolotin, A.Morozov and Sh.Shakirov
Higher nilpotent analogues of A-infinity structure
Phys.Lett.B 651 (2008) 71-73
<https://doi.org/10.1016/j.physletb.2007.05.022>
<http://arxiv.org/abs/0704.2884>
- 50 V.Dolotin, A. Morozov and Sh.Shakirov
A-infinity structure on simplicial complexes
Theor. Math. Phys. 156 (2008) 965-995
<https://doi.org/10.1007/s11232-008-0093-9>
<http://arxiv.org/abs/0704.2609>
- 51 Sh. Shakirov
Higher discriminants of binary forms
Theor. Math. Phys. 153 (2007) 1477-1486
<https://doi.org/10.1007/s11232-007-0129-6>
<http://arxiv.org/abs/math.AG/0609524>

Hirsch publication index:

H-index = 18 via Scopus, <https://www.scopus.com/authid/detail.uri?authorId=23019630900>

H-index = 19 via InspireHEP, <http://inspirehep.net/author/profile/S.Shakirov.1>

Schools and Conferences

- 2023 16th MSJ-SI School and Workshop "Elliptic Integrable Systems, Representation Theory and Hypergeometric Functions" (Tokyo, Japan)
- 2021 Workshop "Randomness, Integrability and Representation Theory in Quantum Field Theory" (Osaka, Japan)
- 2019 String-Math Conference (Uppsala, Sweden)
- 2019, organizer Workshop "Mathematics and Physics of Knots" (Stockholm, Sweden)
- 2018 Conference "Current Progress in Mathematical Physics" (Cambridge, USA)
- 2017 Conference "Progress in Quantum Field Theory and String Theory II" (Osaka, Japan)
- 2016 5th Workshop on Combinatorics of Moduli Spaces (Moscow, Russia)
- 2015 2015 Program "Knot homologies, BPS states, and SUSY gauge theories" (Stony Brook, USA)
- 2014 2014 Summer Simons Workshop in Mathematics and Physics (Stony Brook, USA)
- 2013 2013 Summer Simons Workshop in Mathematics and Physics (Stony Brook, USA)
- 2013 Summer School on Link Homology (Montreal, Canada)
- 2013 String-Math Conference (Stony Brook, USA)
- 2012 Workshop on Tensors and their Geometry (Berkeley, CA)
- 2011 2011 Summer Simons Workshop in Mathematics and Physics (Stony Brook, USA)
- 2010 3rd Workshop on Geometric Methods in Theoretical Physics (Trieste, Italy)
- 2009 2nd Workshop on Geometric Methods in Theoretical Physics (Trieste, Italy)
- 2009 Second International Conference on String Field Theory and Related Aspects (Moscow)
- 2008 46rd International School of Subnuclear Physics (Erice, Italy)
- 2008 Workshop on Geometric Methods in Theoretical Physics (Trieste, Italy)
- 2005 43rd International School of Subnuclear Physics (Erice, Italy)
- 2005 4th International Workshop "Quantum Particles and Fields" (Baku)
- 2004 - 2009 IV,V,VI,VII,VIII International Schools ITF-ITEP (Kiev)
- 2004 XVI International Summer Petrov School (Kazan)

Teaching Experience

Course Instructor,
"Combinatorial Methods in Mathematical Physics",
Moscow Institute of Physics and Technology, Moscow, Fall 2009

Mentoring undergraduate student research,
Moscow Institute of Physics and Technology, Moscow, Spring 2010

Graduate Student Instructor,
"Methods of Mathematics: Calculus, Statistics, and Combinatorics",
University of California, Berkeley, Math 10A, Fall 2014, Prof. Per Persson

Course Instructor,
"Matrix models at finite N ",
University of Geneva, Switzerland, Spring 2022

Personal Information

Date and place of birth: January 8th, 1986, Kazan, Russia

Citizenship: Russia

Civil Status: Single

Languages: Russian (native), English (fluent), German (basic)